

# Formal Methods will not Prevent Self-Driving Cars from Having Accidents

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# From Mobile Robots to Self-Driving Cars



Shakey [66-72]



Darpa Urban Challenge [Nov. 07]



# Why Self-Driving Cars?

[Google Official Blog](#): **What we're driving at**, S. Thrun, 9 October 2010

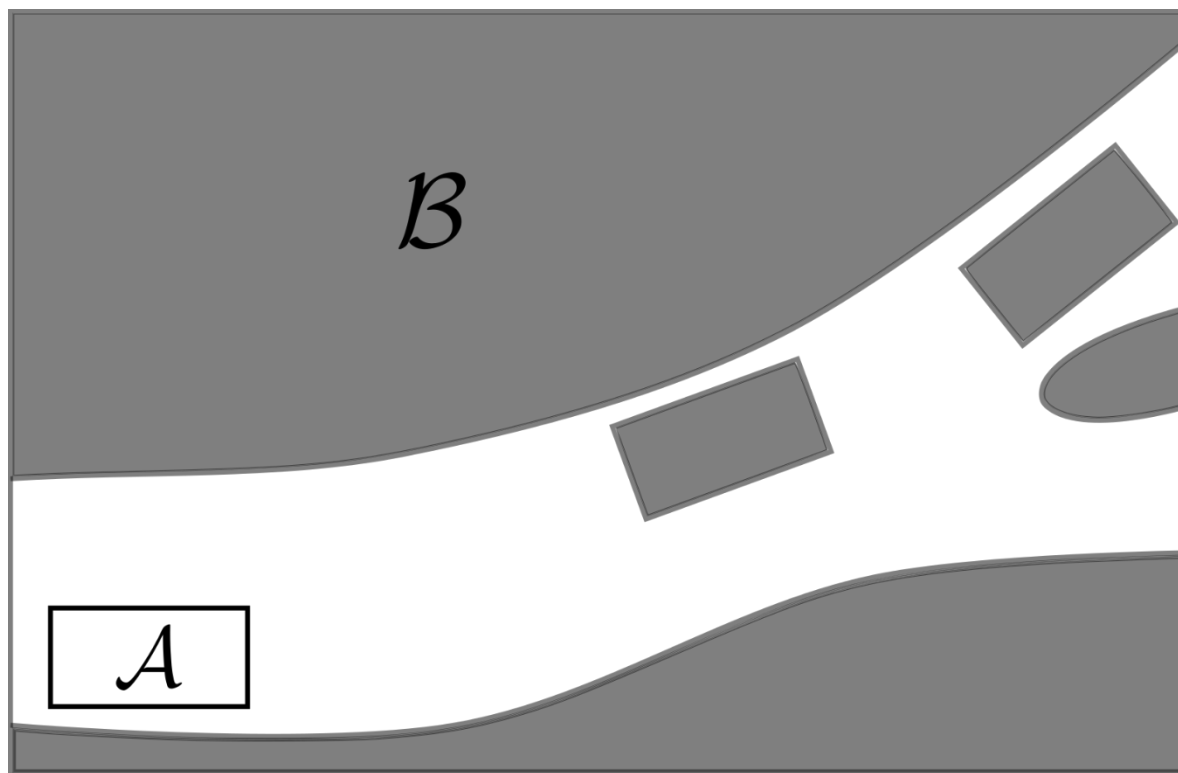
*“Larry and Sergey founded Google because they wanted to help solve really big problems using technology. And one of the big problems we're working on today is **car safety** and efficiency. Our goal is to help **prevent traffic accidents**, free up people's time and reduce carbon emissions by fundamentally changing car use.*

...

***Safety** has been our first priority in this project...”*

2014: **1.25 million deaths** worldwide (**94% human errors** in the US)

# “Absolute” Motion Safety for Self-Driving Cars

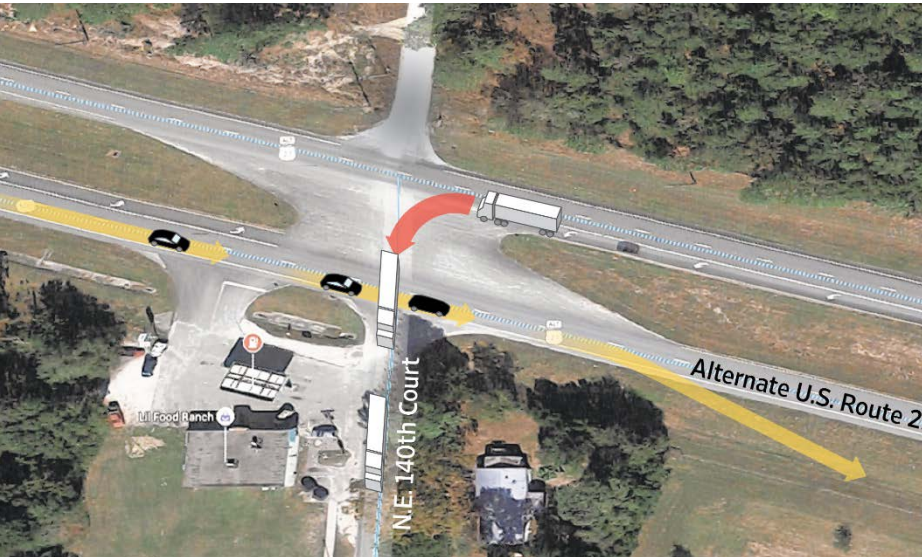


Self-driving car  $\mathcal{A}$ , roadway “objects”  $\mathcal{B}$ :  $\forall t \in [0, \infty], \mathcal{A}(t) \cap \mathcal{B}(t) = \emptyset$

# Self-Driving Cars and Accidents



# A Fatal Misunderstanding



Tesla Model S crash in “Autopilot” mode, May 2016

The sensors failed to differentiate the white side of the tractor trailer against a brightly lit sky...

# A Harmless Misreasoning



[Google Self-Driving Car Project Monthly Report, February 2016](#)

*“Our car had detected the approaching bus, but predicted that it would yield to us because we were ahead of it.”*

# Why Collisions Happen?

- Hardware failures
  - Software bugs
  - Misunderstanding
  - Misreasoning
- 
- Focus on **misreasoning** in **dynamic** environments
  - Can **motion safety** be guaranteed?



# Outline of the Talk

## **1. Case study**

Gaining insight into motion safety

## **2. Inevitable collision states**

Furthering the analysis in a formal framework

## **3. Motion safety in the real world**

Houston, we have a problem

## **4. Weaker motion safety levels**

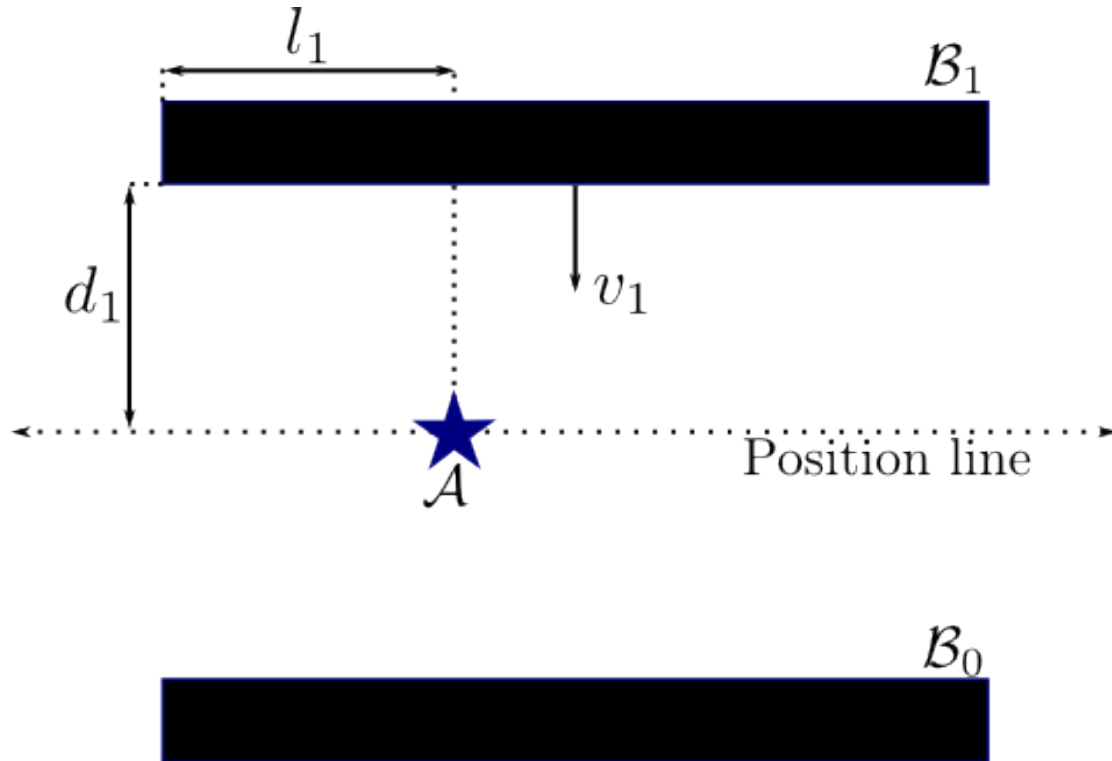
Less is better than nothing

# 1

## Case Study

*Gaining insight into motion safety*

# The “Compactor” Scenario



$$A : \dot{p} = v, |v| \leq v_{\max}$$

- Reasoning about the **future**

- ✓ Collision time

$$t_c = d_1/v_1$$

- ✓ Escape time

$$\delta_e = l_1/v_{\max}$$

- Limited **decision time**

$$\delta_d < t_c - \delta_e$$

- Appropriate **time horizon**

$$\delta_h > \delta_d + \delta_e$$

# 2

## Inevitable Collision States

*Furthering the analysis in a formal framework*

# Inevitable Collision States *[Fraichard 03]*

- Collision States (CS) vs. Inevitable Collision States (ICS):

*Whatever the future trajectory of the robot, a collision will happen*

$\mathcal{A}$ : state  $s \in \mathcal{S}$ , control  $u \in \mathcal{U}$ , trajectory:  $\pi : [t_0, \infty] \longrightarrow \mathcal{U}$

State  $s_0$  is:

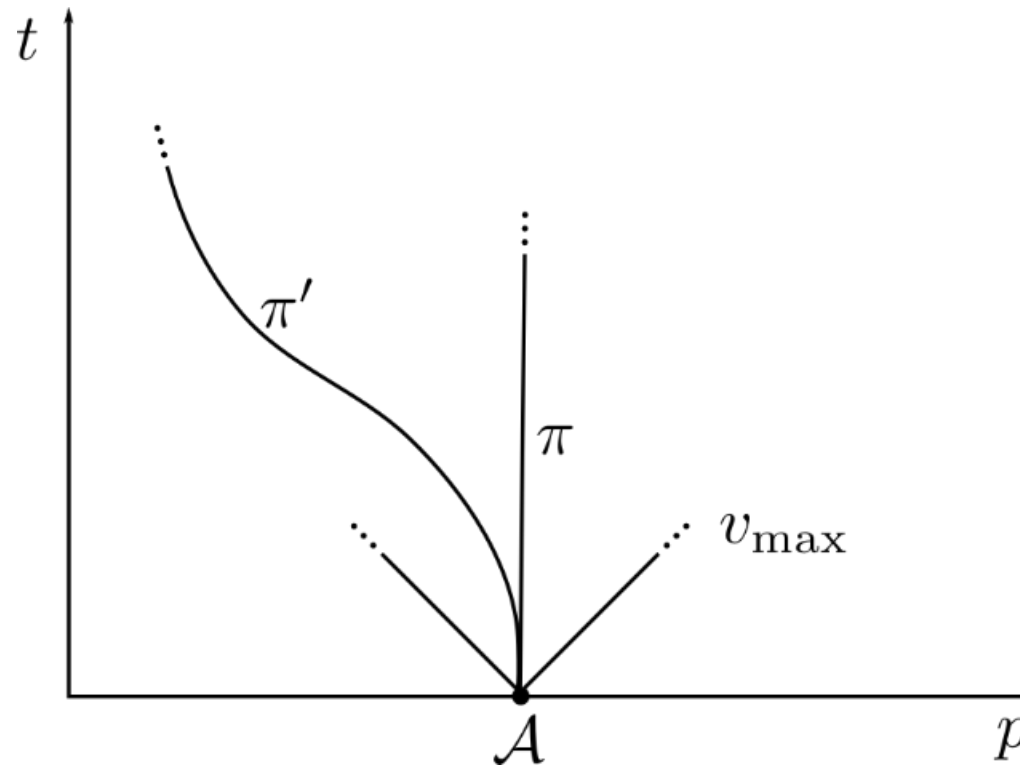
$$\text{CS} : \mathcal{A}(s_0(t)) \cap \mathcal{B}(t) \neq \emptyset$$

$$\text{ICS} : \forall \pi, \exists t \in [0, \infty], s(s_0, \pi, t) \in \text{CS}$$

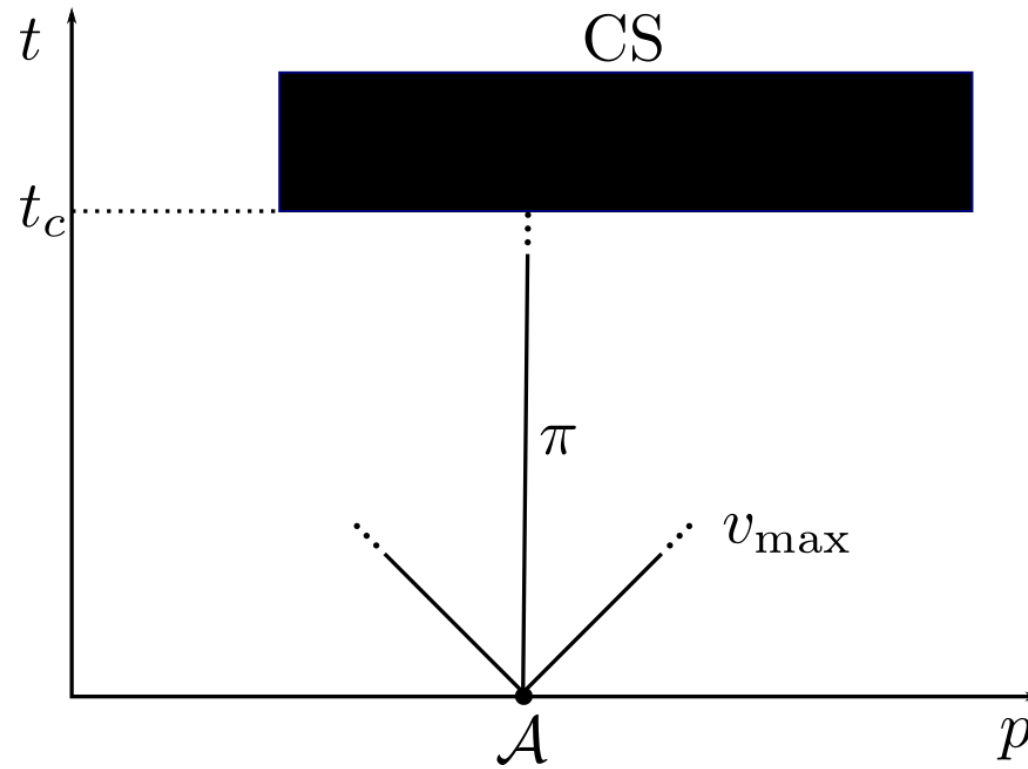
$$\text{(Absolutely) Safe} : \exists \pi, \forall t \in [0, \infty], s(s_0, \pi, t) \notin \text{CS}$$

- Key to motion safety: **stay away from ICS**

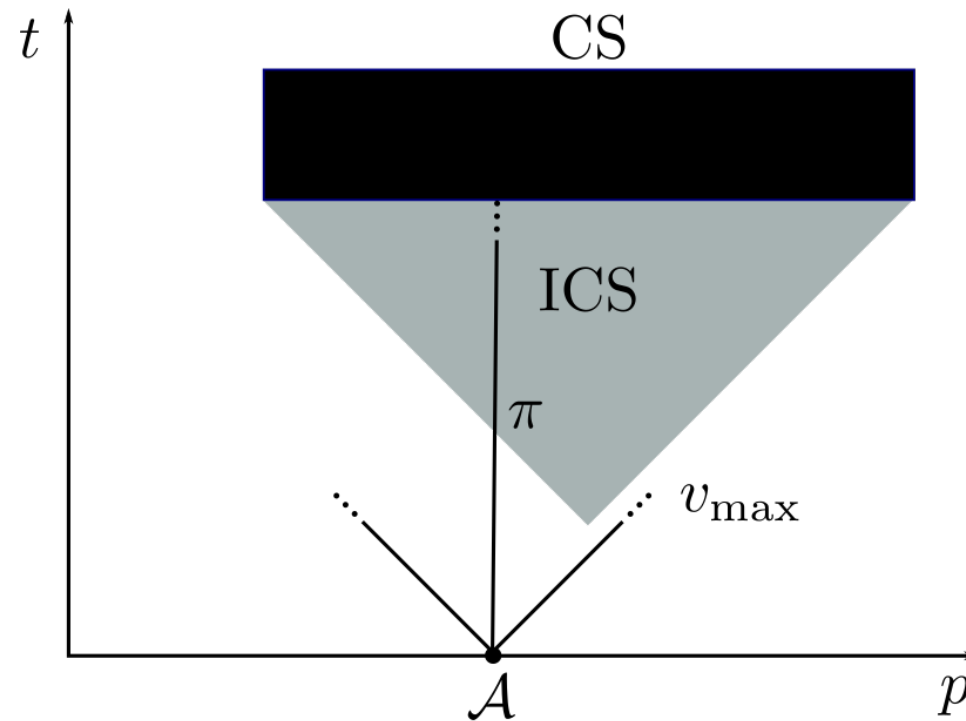
# From Cartesian Space to State-Time Space



# Collision States



# Inevitable Collision States





# Inevitable Collision States' Teachings

1. Obstacles are not independent

$$ICS(\bigcup_i \mathcal{B}_i) \supseteq \bigcup_i ICS(\mathcal{B}_i)$$

2. Decision time

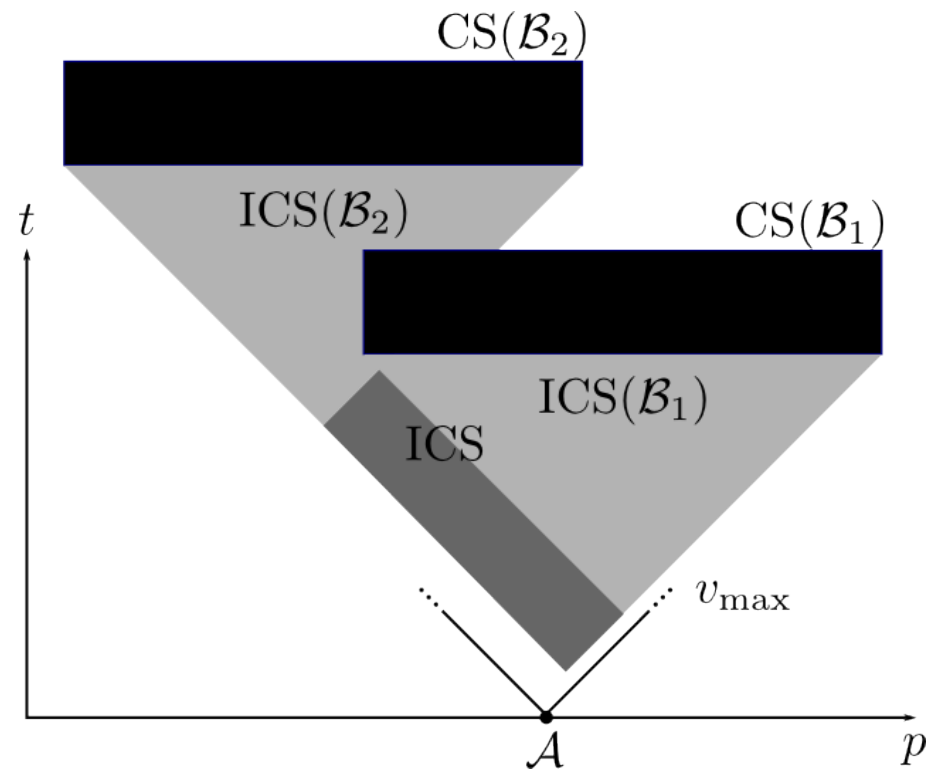
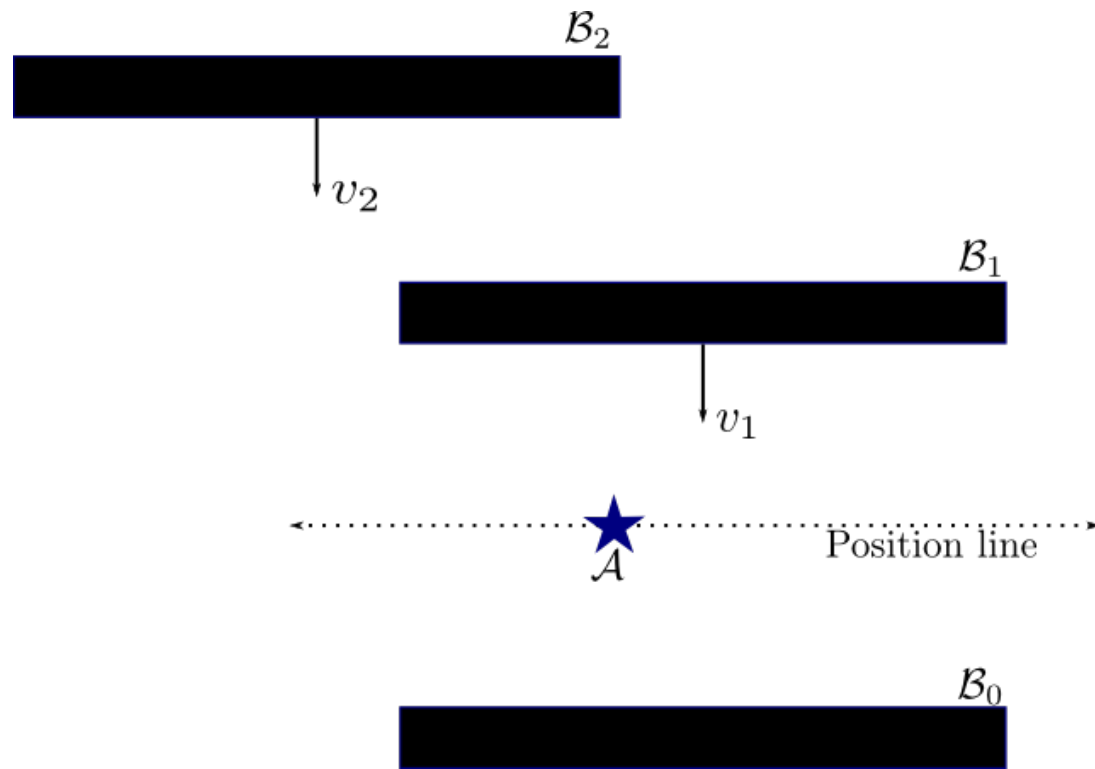
$\delta_d = t_c | s(s_0, \pi, t_c) \in ICS$ , where  $\pi$  is the current trajectory

3. Time Horizon

$$\delta_h = t_h | ICS(\mathcal{B}[0, \infty]) \subseteq ICS(\mathcal{B}[0, t_h])$$

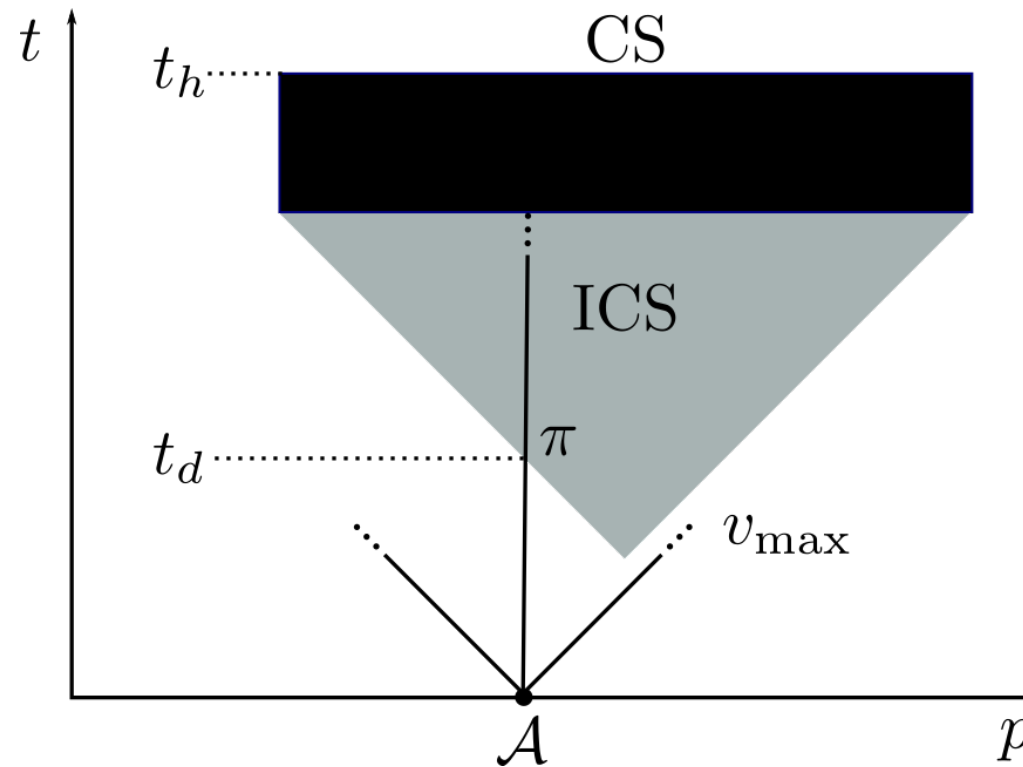
Static/freezing/periodic environments  $\Rightarrow \delta_d$  not infinite

# Obstacles are not Independent



$$\text{ICS}(\mathcal{B}_1 \cup \mathcal{B}_2) \supseteq \text{ICS}(\mathcal{B}_1) \cup \text{ICS}(\mathcal{B}_2)$$

# Decision Time and Time Horizon



$$\begin{cases} \delta_d = t_d \\ \delta_h = t_h \text{ since } ICS(\mathcal{B}[0, \infty]) \subseteq ICS(\mathcal{B}[0, t_h]) \end{cases}$$

# What Have We Learned?

1. Global reasoning about the future evolution of the environment until an appropriate time horizon  $\delta_h$ , limited decision time  $\delta_d$
2. Absolute motion safety = stay away from ICS
3.  $ICS = f(CS[0, \delta_d])$
4.  $CS = g(B[0, \delta_d])$
5.  $\delta_d$  infinite (except for static/freezing/periodic environments)

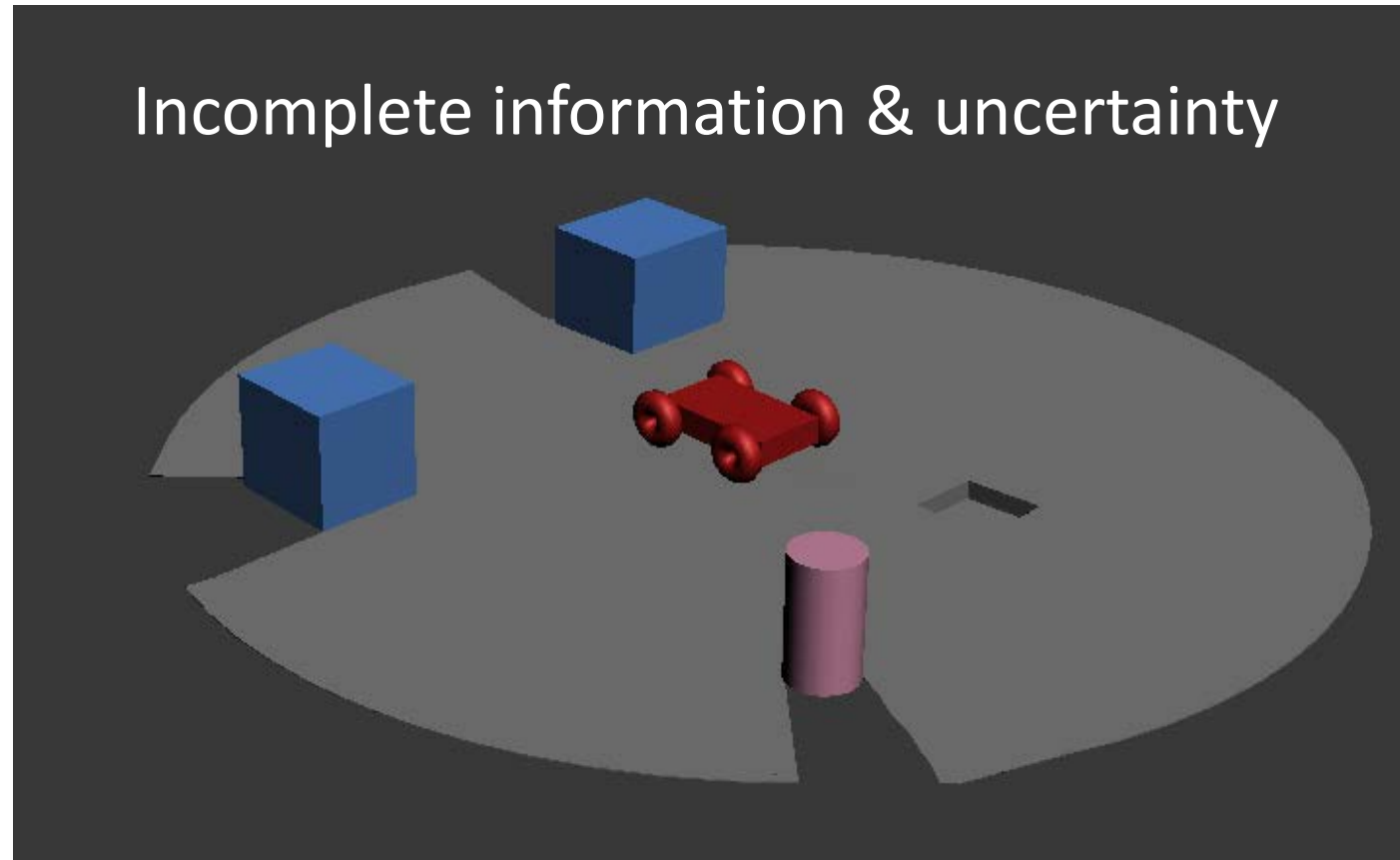
*[Martinez & Fraichard 08]*: robot controller in a static/freezing/periodic environment  $\Rightarrow$  **guaranteed absolute motion safety**

# 3

## Motion Safety in the Real World

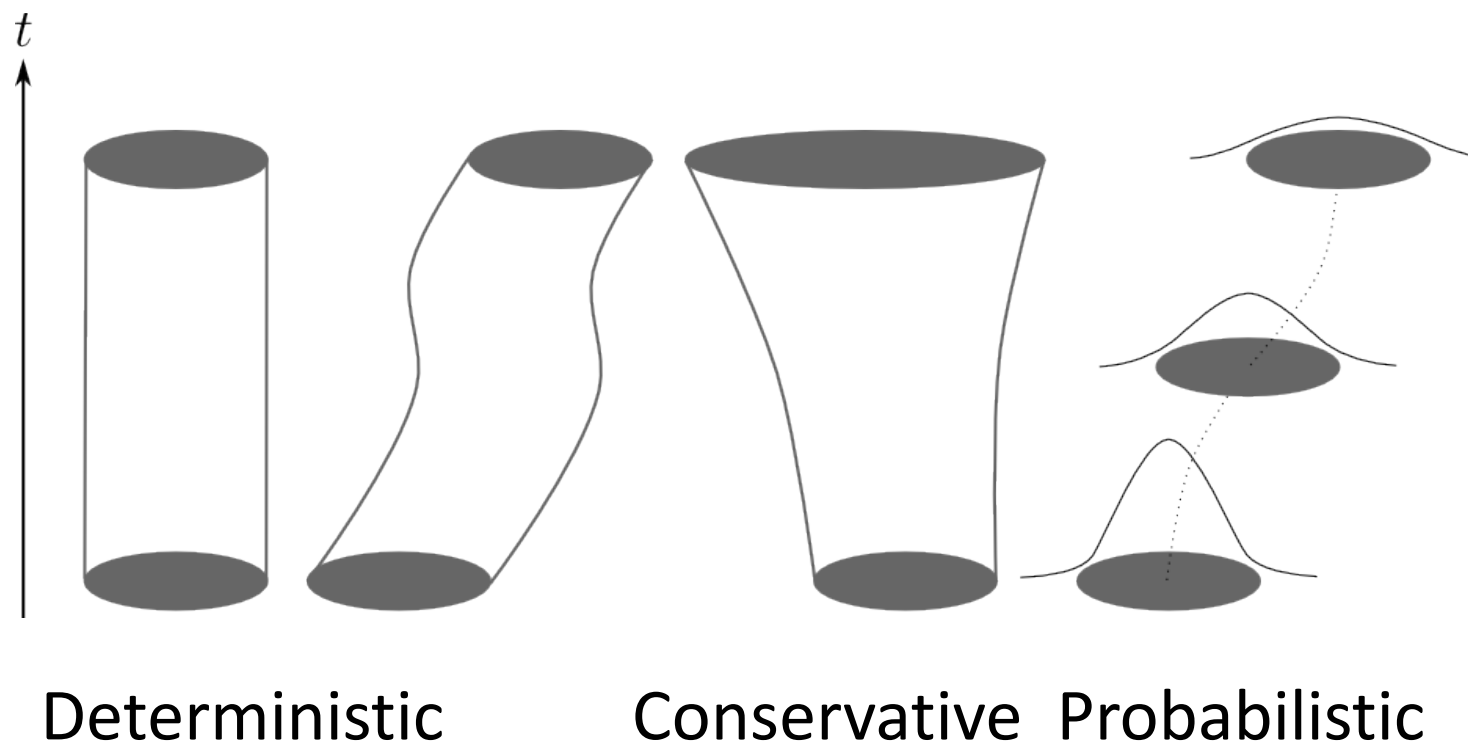
*Houston, we have a problem*

# What about Real World Situations?



$$\mathcal{B}[0, \infty]?$$

# Modeling the Future



# Consequences wrt. Motion Safety

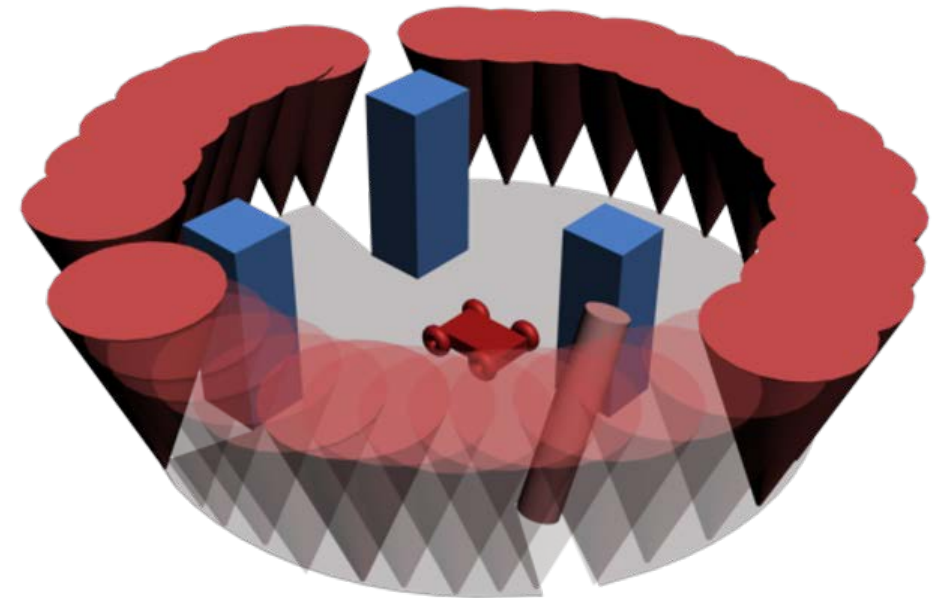
- For guaranteed motion safety:

**Conservative model**

➤ Every state is an *ICS* ( $\delta_h = \infty$ )

- What can be done then?

...**Weaker** motion safety levels





# 4

**Weaker Motion Safety Levels**  
*Less is better than nothing*

# Passive Motion Safety

- Should a collision take place, the robot will be at rest
- Braking ICS [*Bouraine & Fraichard, 11*]

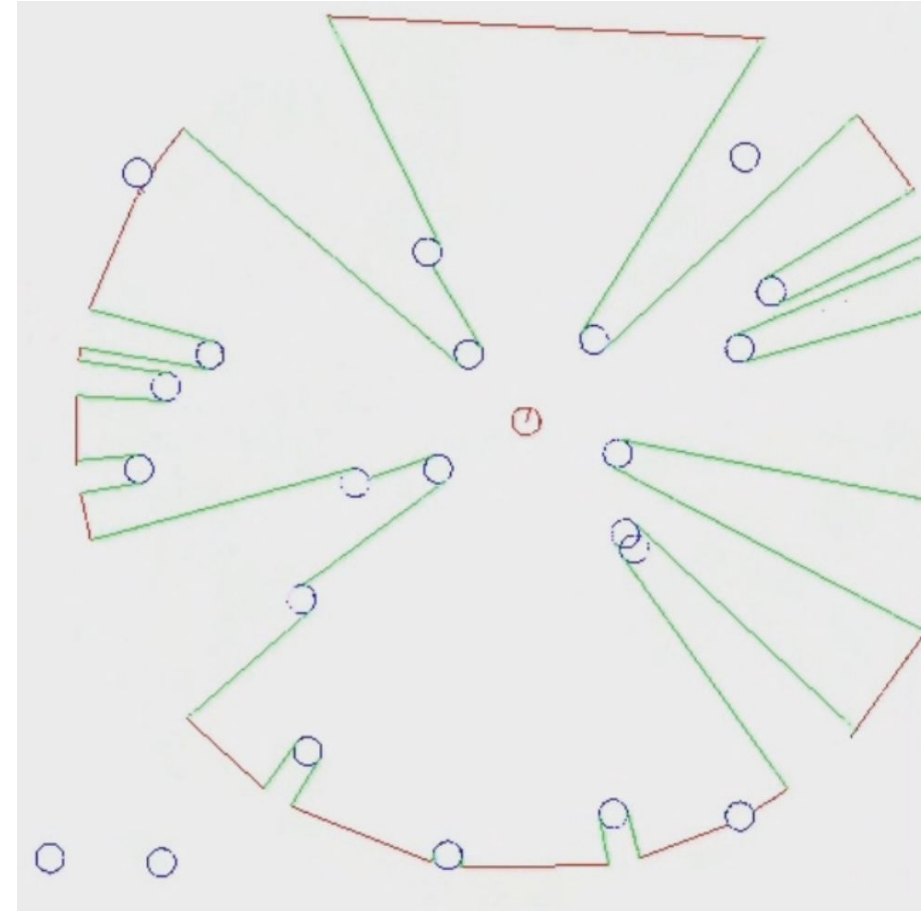
$\mathcal{A}$ : state  $s \in \mathcal{S}$ , control  $u \in \mathcal{U}$ , braking trajectory:  $\pi_b : [t_0, t_b] \longrightarrow \mathcal{U}$

State  $s_0$  is a Braking ICS iff  $\forall \pi_b, \exists t \in [0, t_b], s(s_0, \pi, t) \in \text{CS}$

- Key to passive motion safety: **stay away from Braking ICS**
- Finite time horizon:  $\max\{t_b\}$
- Everybody enforces it  $\Rightarrow$  no collision at all

# Passive Motion Safety can be Guaranteed

- [Provably Safe Navigation for Mobile Robots with Limited Field-of-Views in Dynamic Environments, Bouraine et al., AR, 12]
  - ✓ Dynamic system
  - ✓ Braking ICS



# What about Formal Methods?

- [Formal Verification of Obstacle Avoidance and Navigation of Ground Robots, Mitsch et al., IJRR, 17]
  - ✓ Hybrid system
  - ✓ Differential dynamic logic

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**Model 1** Dynamic window with passive safety

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$$dw_{ps} \equiv (ctrl; dyn)^* \quad (1)$$

$$ctrl \equiv ctrl_o \parallel ctrl_r \quad (2)$$

$$ctrl_o \equiv v_o := (*, *); ?\|v_o\| \leq V \quad (3)$$

$$ctrl_r \equiv (a_r := -b) \quad (4)$$

$$\cup (?v_r = 0; a_r := 0; \omega_r := 0) \quad (5)$$

$$\cup (a_r := *; ?-b \leq a_r \leq A; \quad (6)$$

$$\omega_r := *; ?-\Omega \leq \omega_r \leq \Omega; \quad (7)$$

$$p_c := (*, *); d_r := (*, *); \quad (8)$$

$$p_o := (*, *); ?curve \wedge safe) \quad (9)$$

$$curve \equiv \|p_r - p_c\| > 0 \wedge \omega_r \|p_r - p_c\| = v_r \quad (10)$$

$$\wedge d_r = \frac{(p_r - p_c)^\perp}{\|p_r - p_c\|}$$

$$safe \equiv \|p_r - p_o\|_\infty > \frac{v_r^2}{2b} + \left(\frac{A}{b} + 1\right) \left(\frac{A}{2}\varepsilon^2 + \varepsilon v_r\right) \quad (11)$$

$$+ V \left(\varepsilon + \frac{v_r + A\varepsilon}{b}\right) \quad (12)$$

$$dyn \equiv (t := 0; p_r^{x'} = v_r d_r^x, p_r^{y'} = v_r d_r^y, \quad (13)$$

$$d_r^{x'} = -\omega_r d_r^y, d_r^{y'} = \omega_r d_r^x, \quad (14)$$

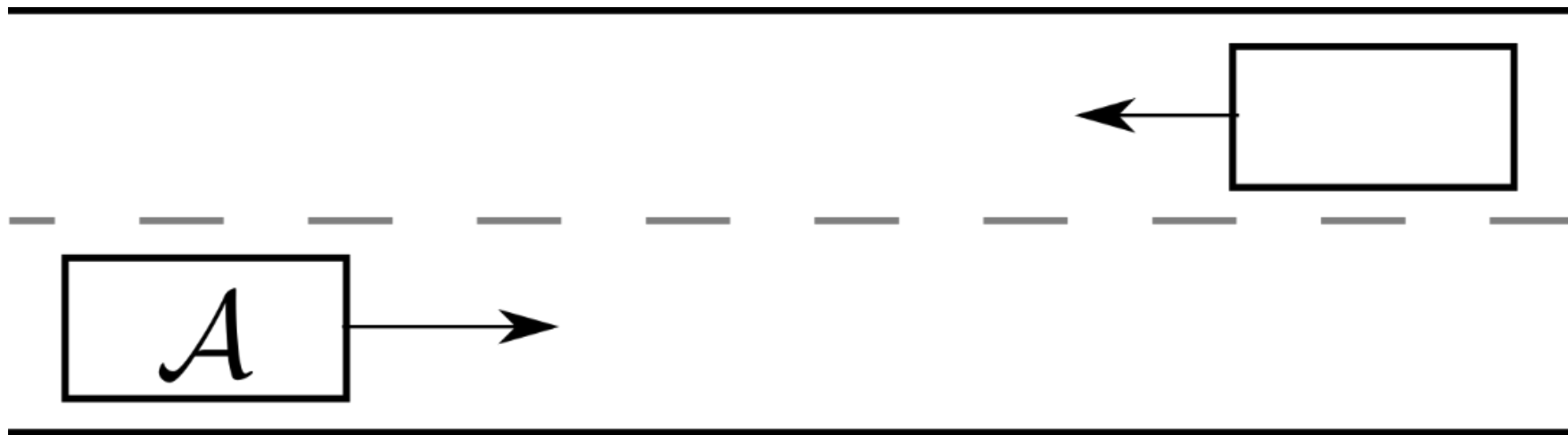
$$p_o^{x'} = v_o^x, p_o^{y'} = v_o^y, \quad (15)$$

$$v_r' = a_r, \omega_r' = \frac{a_r}{\|p_r - p_c\|}, t' = 1 \quad (16)$$

$$\& v_r \geq 0 \wedge t \leq \varepsilon) \quad (17)$$


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# Passive Motion Safety and Self-Driving Cars



# Time to Conclude

- In the real world, forget guaranteed absolute motion safety
  - Guaranteed lesser motion safety possible but...
  - Possible improvements: V2V, V2I, roadway engineering
  
  - Self-Driving cars: ~1.4 million miles (Google, up until now), 1 death
  - Regular cars: ~3 trillion miles, 30 057 deaths (USA, 2014)
  - 1 death/100 million miles
- Technology still has to prove itself...