

# Development and Formal Verification of a Flight Stack for a High-Altitude Micro Glider

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Toulouse, 10.10.2017



<https://www.brightwork.com/blog/project-failures-boeings-787-dreamliner>

## Rejected because considered to ...

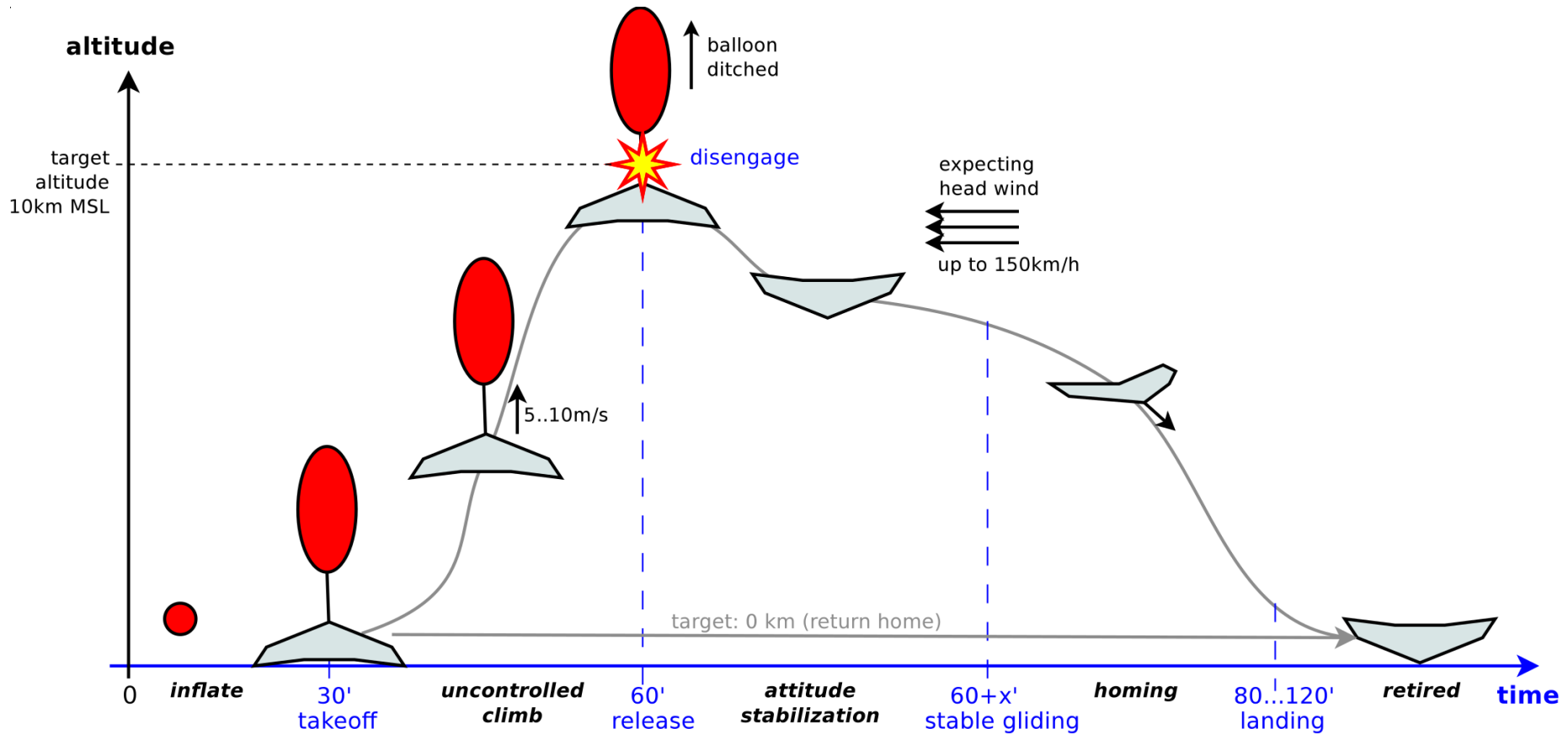
- require a lot of additional specification
- require user interaction; little automation
- require experts; results are difficult to understand

?

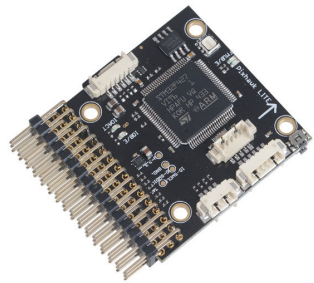
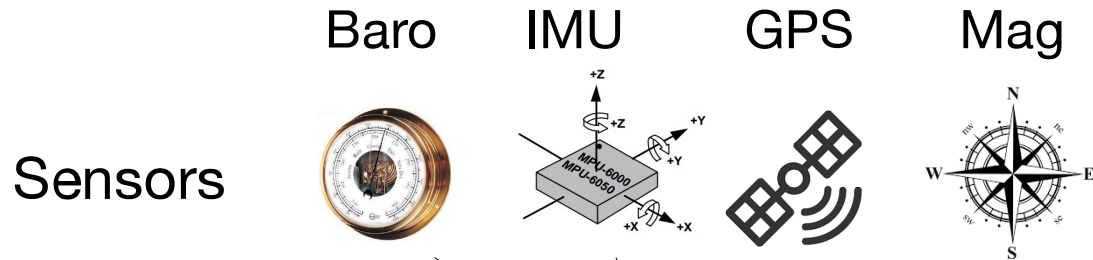
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?

# Mission – Novel Weather Balloon



# Introduction to the Scenario

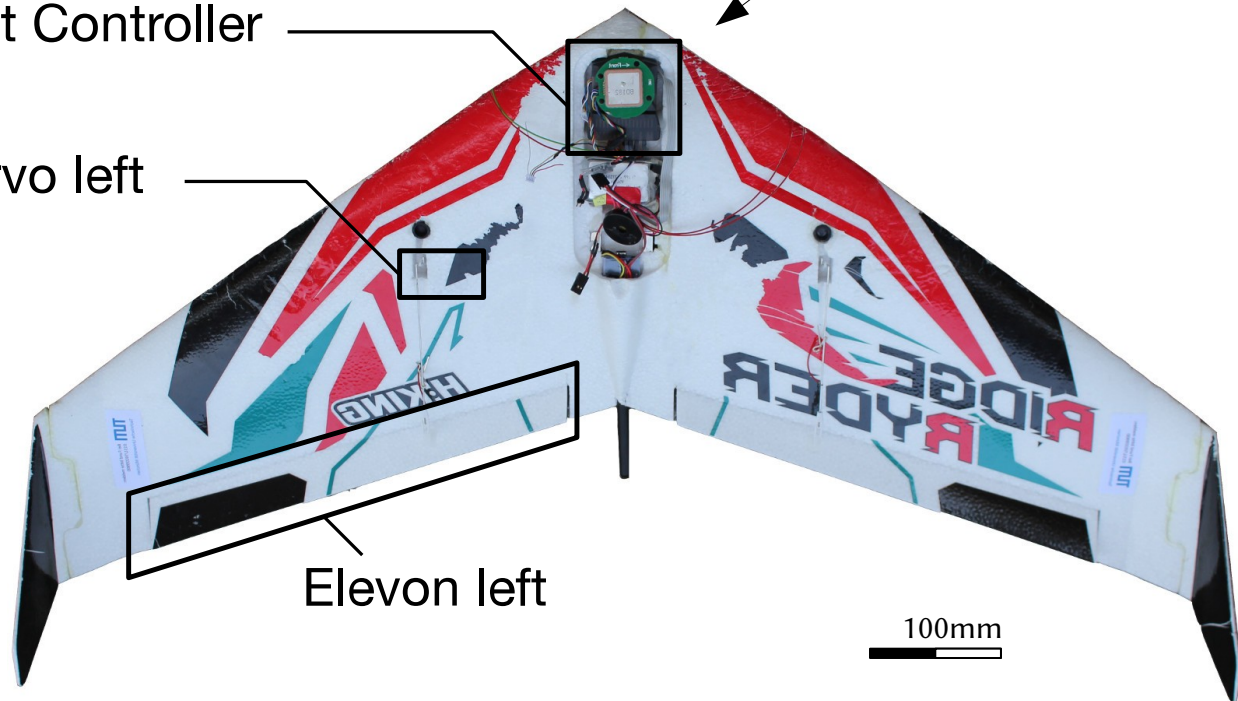


Flight Controller

Servo left



Elevon left

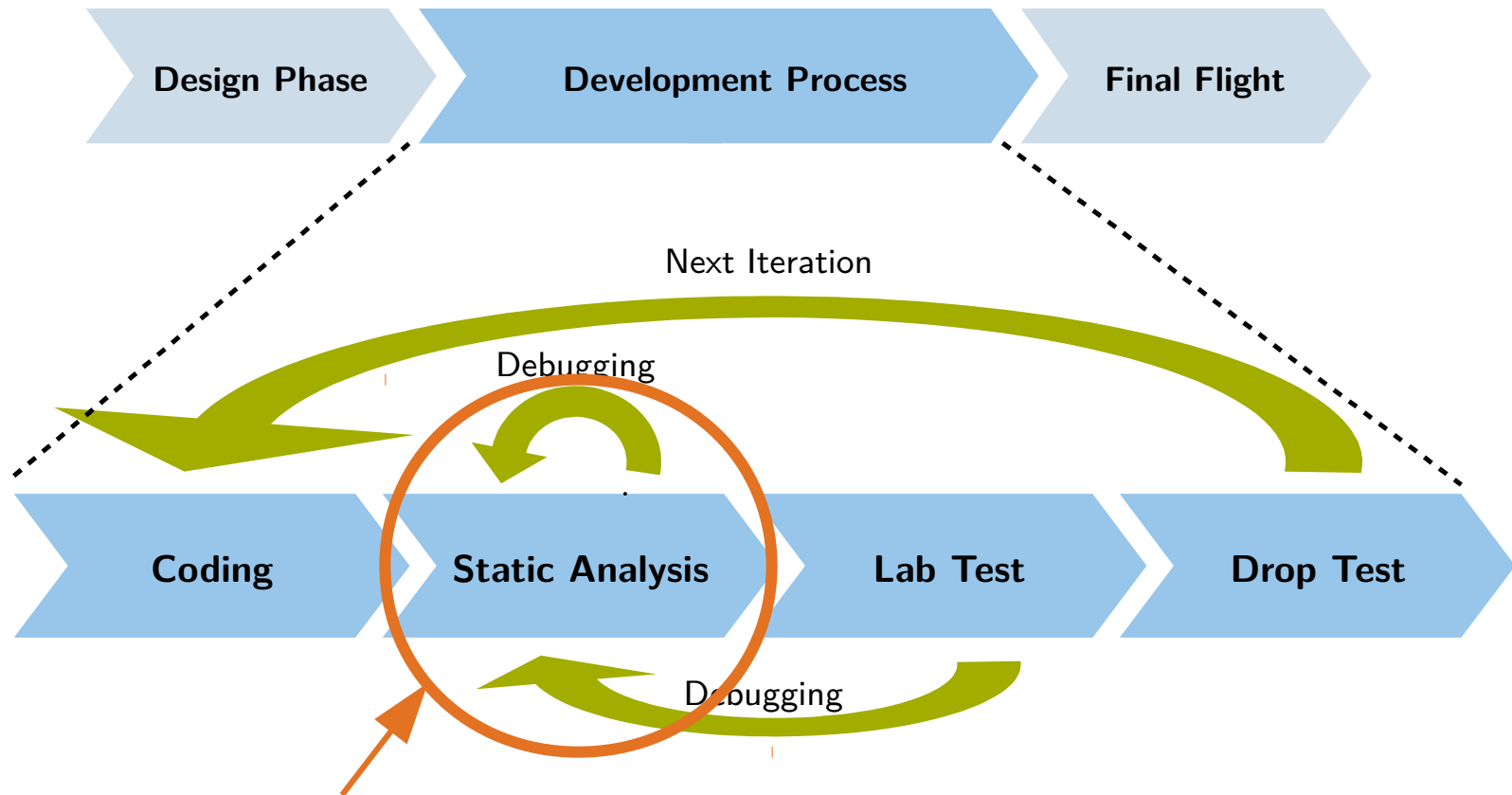


100mm

# The Roll of System Testing

- Full system tests, including external effects (wind, etc..)
- Risky and high effort (Time&Money)  $\Rightarrow$  as little as possible
- Germany: Must not fly above 100m AGL  $\Rightarrow$  limited





1. Fast: before compiling
2. Normal: Continuous Integration with git
3. Nightly “deep” verification runs with long timeouts



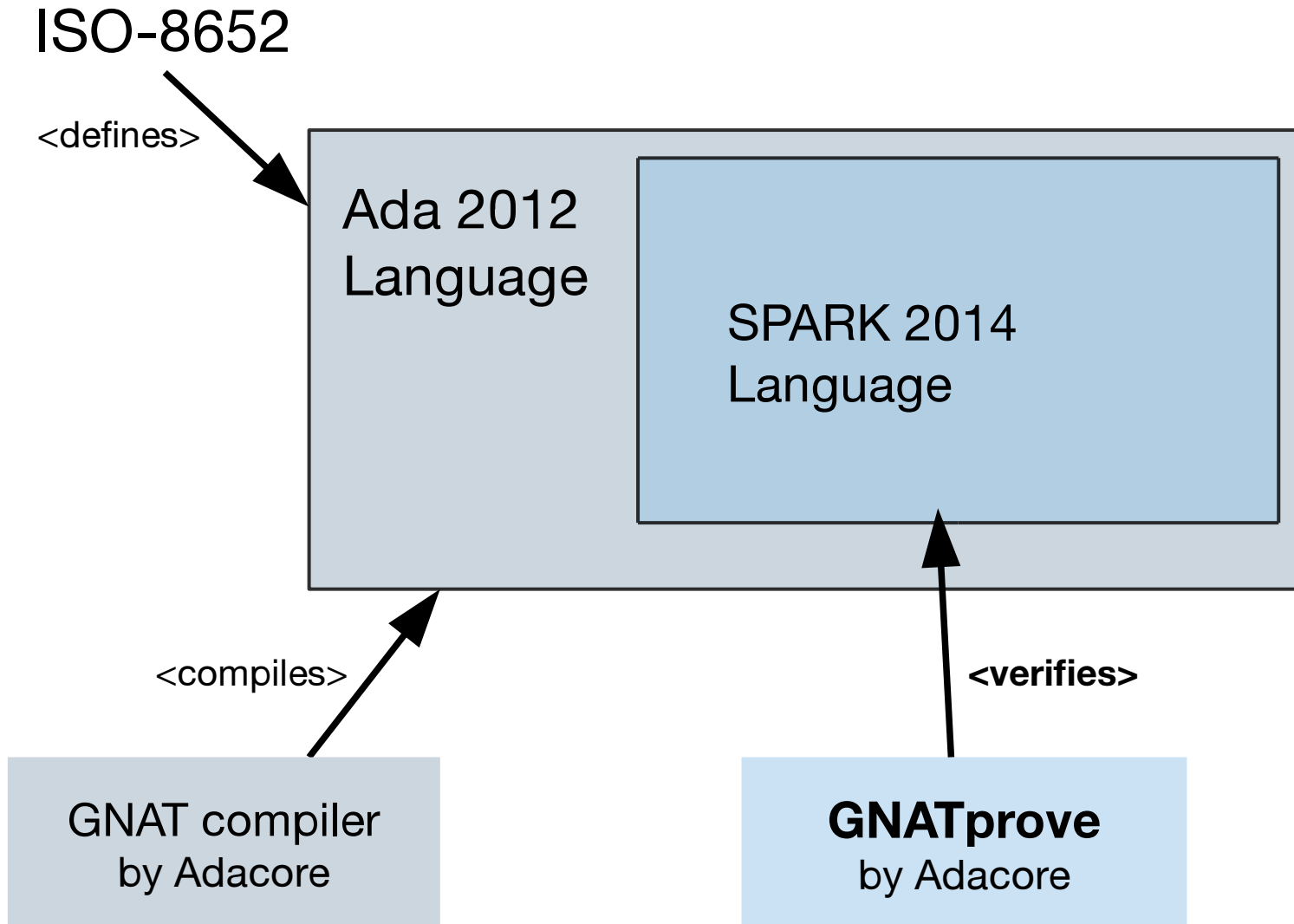
Static Analysis

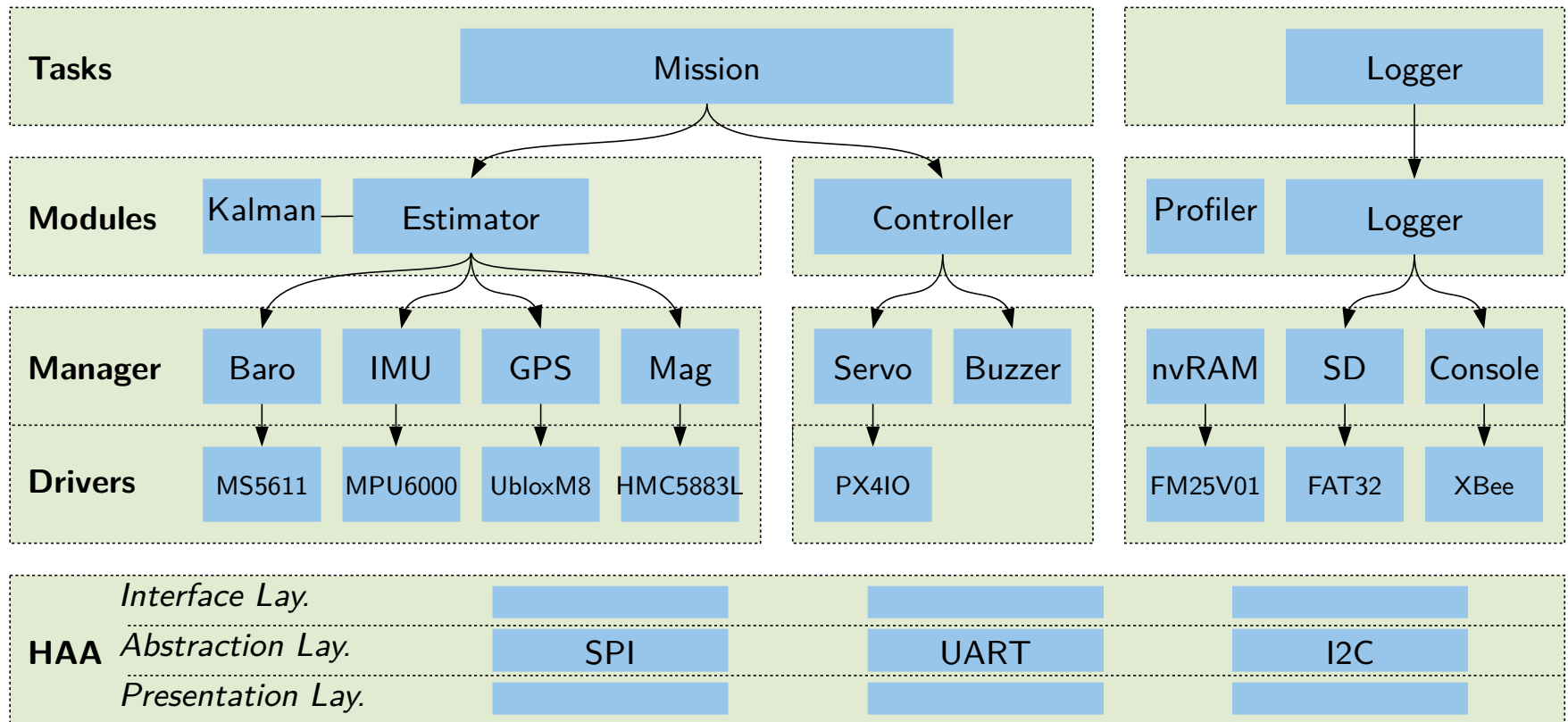
System Testing

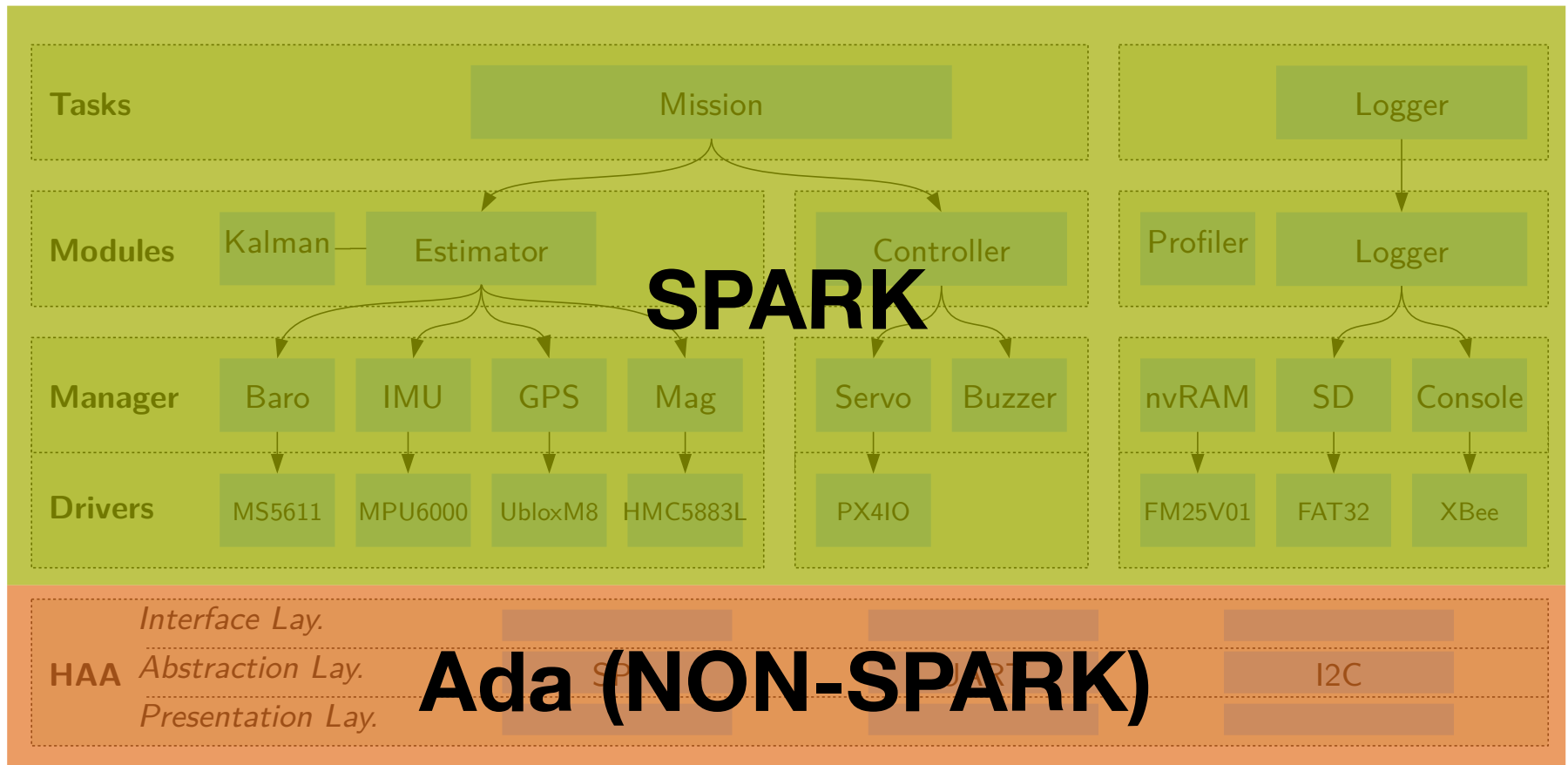
Operation

- most by static analysis (each developer & nightly runs)
  - replace unit testing
  - identify under-specification
- few by system testing
  - defects which were missed by static analysis
  - defects which require context beyond source code
  - logging of exceptions: no reproduction issues
- none during operation
  - nevertheless: logging of exceptions & in-air reset









We want to formally verify

## **Absence of run-time errors**

Division by zero, overflows

## **Integration Correctness**

Valid inputs and outputs

## **Functional Behavior**

Input to output relation

## **Information Flow**

Global variables,  
Input to output dependencies

## **Physical Dimensions**

Compliance with  
physical laws

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```
1 package MyPack with SPARK_Mode is
2
3   subtype Percentage is Natural;
4
5   Global_Ratio : Percentage;
6
7   procedure set_ratio( alt, maxalt : Integer )
8   is begin
9     Global_Ratio := alt * 100 / maxalt;
10  end set_ratio;
11
12 end MyPack;
```

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```

MyPack:9:35 medium: overflow check might fail

MyPack:9:41 medium: divide by zero might fail

MyPack:9:41 medium: range check might fail

```
1 package MyPack with SPARK_Mode is
2
3   subtype Percentage is Natural;
4
5   Global_Ratio : Percentage;
6
7   procedure set_ratio( alt, maxalt : Integer ) with
8     Pre => alt,maxalt > 0 and alt < Integer'Last/100
9   is begin
10    Global_Ratio := alt * 100 / maxalt;
11  end set_ratio;
12
13  set_ratio( 42, 62 );
14 end MyPack;
```



```
1 package MyPack with SPARK_Mode is
2
3   subtype Percentage is Natural;
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7   procedure set_ratio( alt, maxalt : Integer ) with
8     Pre => alt,maxalt > 0 and alt < Integer'Last/100
9   is begin
10    Global_Ratio := alt * 100 / maxalt;
11  end set_ratio;
12
13  set_ratio( 42, 62 );
14 end MyPack;
```

Mypack:10:35 info: overflow check proved

Mypack:10:41 info: division check proved

Mypack:10:41 info: range check proved

Mypack:13:3 info: Precondition proved

```
1 package MyPack with SPARK_Mode is
2
3   subtype Tar_Alt is Integer range 10 .. 10_000;
4   subtype Alt is Integer range 0 .. 100_000;
5   subtype Percentage is Natural;
6
7   Global_Ratio : Percentage;
8
9   procedure set_ratio( val : Alt; max : Tar_Alt )
10  is begin
11    Global_Ratio := val * 100 / max;
12  end set_ratio;
13
14 end MyPack;
```

```
1 package MyPack with SPARK_Mode is
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```

Mypack:11:35 info: overflow check proved

Mypack:11:41 info: division check proved

Mypack:11:41 info: range check proved

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```
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4
5   Global_Ratio : Percentage;
6
7   procedure set_ratio( alt, maxalt : Integer )
8   is begin
9     Global_Ratio := alt * 100 / maxalt;
10  end set_ratio;
11
12 end MyPack;
```

MyPack:9:19 info: initialization of "Global\_Ratio" proved

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**Scientific:** angular rate = 20 deg / 100 ms = 200 deg/s

C Program:

```
1 Float angle = 20;  
2 Float dt    = 0.1;  
3  
4 Float rate = dt / angle;
```

SPARK Program:

```
1 angle : Angle_Type := 20.0 * Degree;           -- Value: 0.524  
2 dt    : Time_Type  := 100.0 * Milli * Second; -- Value: 0.100  
3 rate  : Angular_Velocity_Type := dt / angle;  
4  
5 yaw   : Angle_Type := 20.0;
```

**Scientific:** angular rate = 20 deg / 100 ms = 200 deg/s

C Program:

```
1 Float angle = 20;  
2 Float dt    = 0.1;  
3  
4 Float rate = dt / angle;
```

SPARK Program:

```
1 angle : Angle_Type := 20.0 * Degree;           -- Value: 0.524  
2 dt    : Time_Type  := 100.0 * Milli * Second; -- Value: 0.100  
3 rate  : Angular_Velocity_Type := dt / angle;  
4  
5 yaw   : Angle_Type := 20.0;
```

Mypack:3:17 dimensions mismatch in assignment

Mypack:3:17 expected dimension [A.T\*\*(-1)], found [T.A\*\*(-1)]

Mypack:5:17 warning: assumed to be "20.0 Rad"

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```
1  -- Functional Requirement
2  function FR_poshold_iff_no_course() return Boolean is (
3      (Have_Course and G_state.mode /= MODE_POSHOLD) or
4      (not Have_Course and G_state.mode = MODE_POSHOLD)
5  ) with Ghost;
6
7  -- Functional Requirement
8  function FR_arrive_iff_near_target() return Boolean is (
9      if (Have_Home_Position and Have_My_Position) then
10         (dist2home < TARGET_R and G_state.mode = MODE_ARRIVED) or
11         (dist2home >= TARGET_R and dist2home <= 2.0*TARGET_R) or
12         (dist2home > 2.0*TARGET_R and G_state.mode /= MODE_ARRIVED)
13     else G_state.mode /= MODE_ARRIVED
14 ) with Ghost;
15
16 -- Update the controller mode, depending on state
17 procedure Update_Homing() with
18     Post => FR_poshold_iff_no_course and FR_arrive_iff_near_target;
```

We want to formally verify

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Input to output relation

## Information Flow

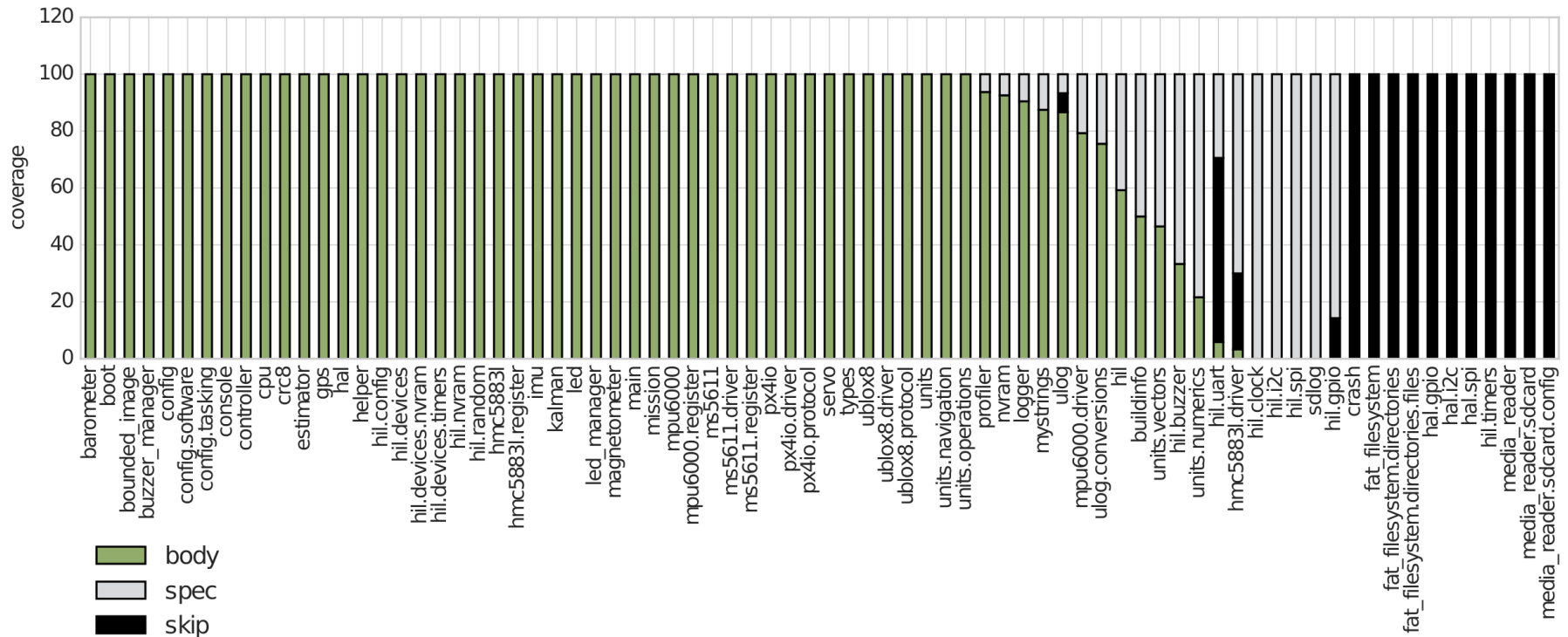
Global variables,  
Input to output dependencies

## Physical Dimensions

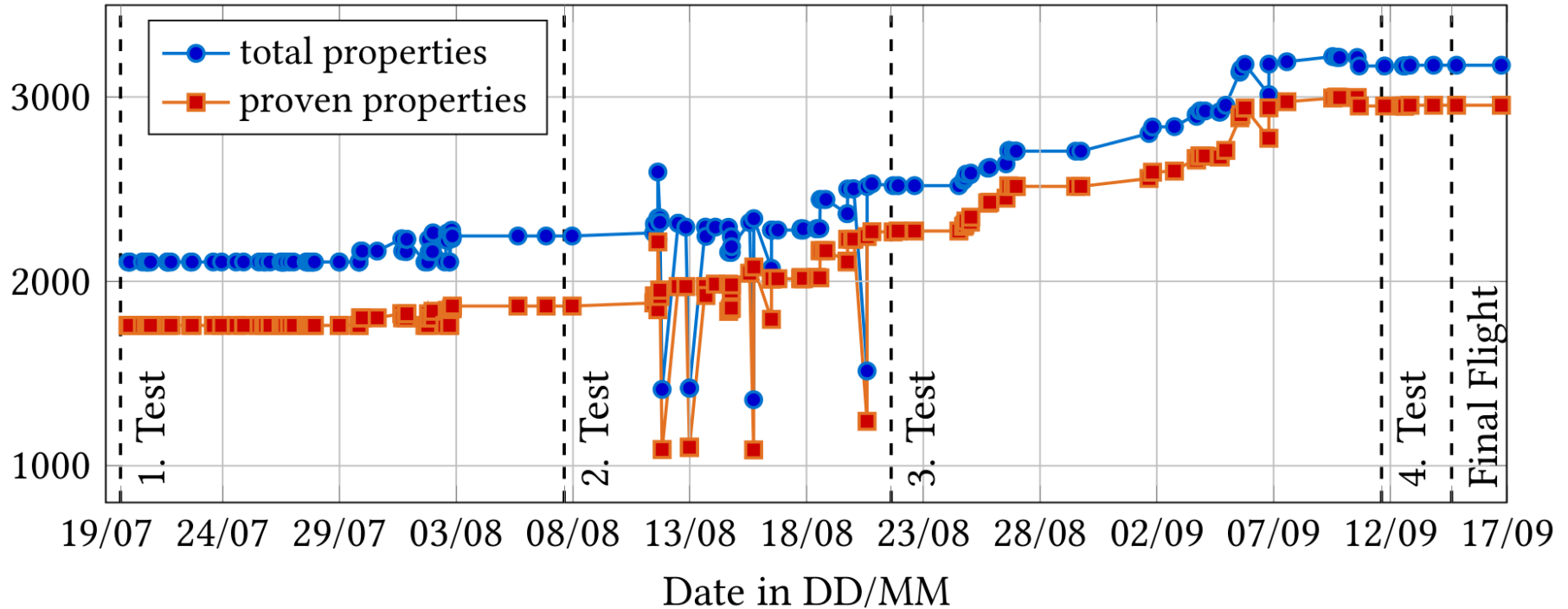
Compliance with  
physical laws

# Final GNATprove Results

- SPARK subprogram coverage: 82%



# Final GNATprove Results





## Totals of verified properties

Absence of  
run-time errors  
**1487 / 1711 (86.9%)**

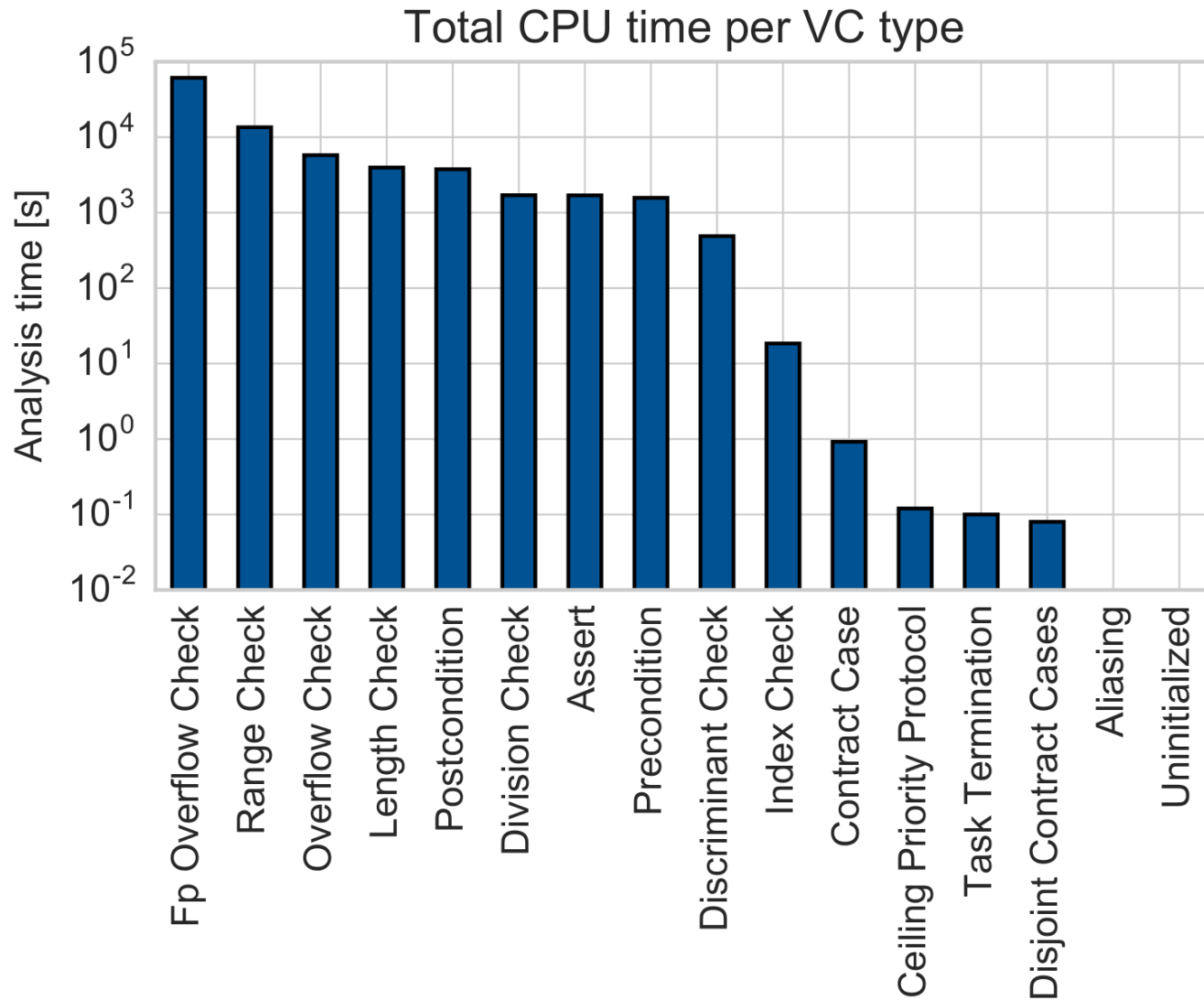
Integration  
Correctness  
**277 / 282 (98.2%)**

Functional  
Requirements  
**2 / 2 (100%)**

Information Flow  
**1539 / 1540 (99.9%)**

Physical Dimensions  
**?/? (100%)**

# Final GNATprove Results

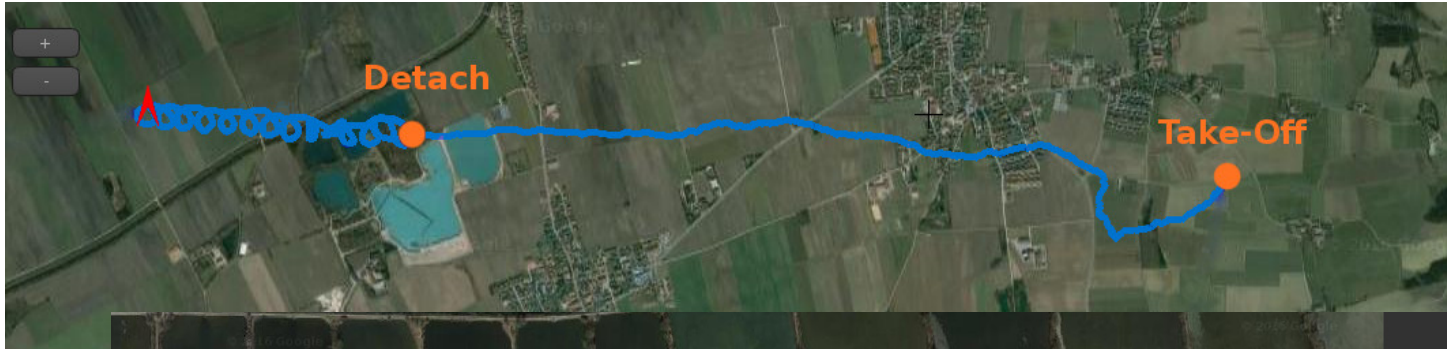


# Final Flight on 2016-09-14

Target Altitude: 6100 m AGL

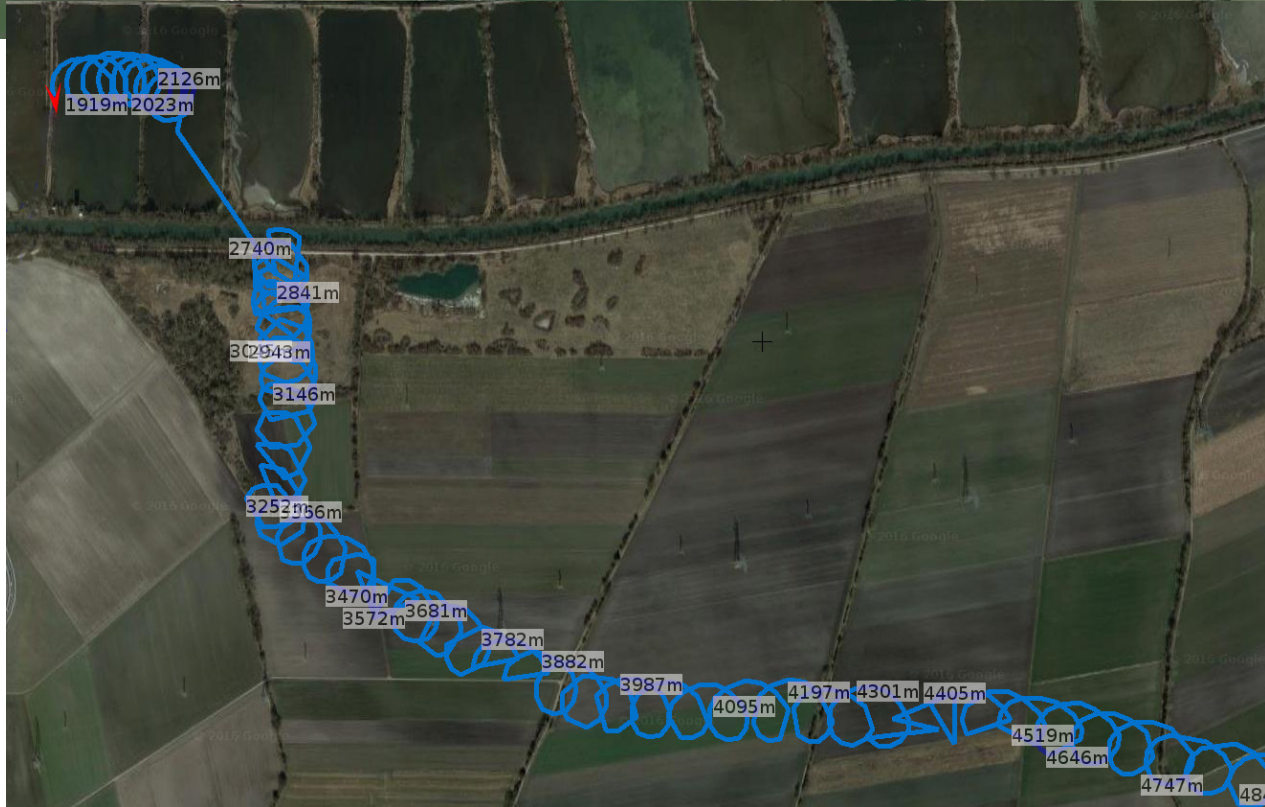


# Final Flight on 2016-09-14



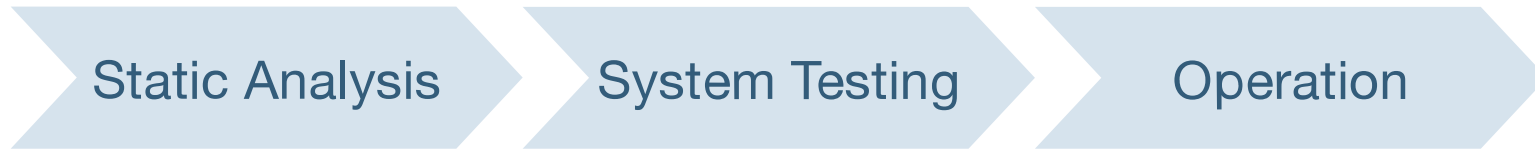
**A/C Status**

|        |         |
|--------|---------|
| Lat    | 11.7479 |
| Lon    | 48.1952 |
| Alt    | 5731.2  |
| Hdg    | 0       |
| G'Vel  | WAIT    |
| AltMSL | 5731.2  |
|        | 3.7474  |



**A/C Status**

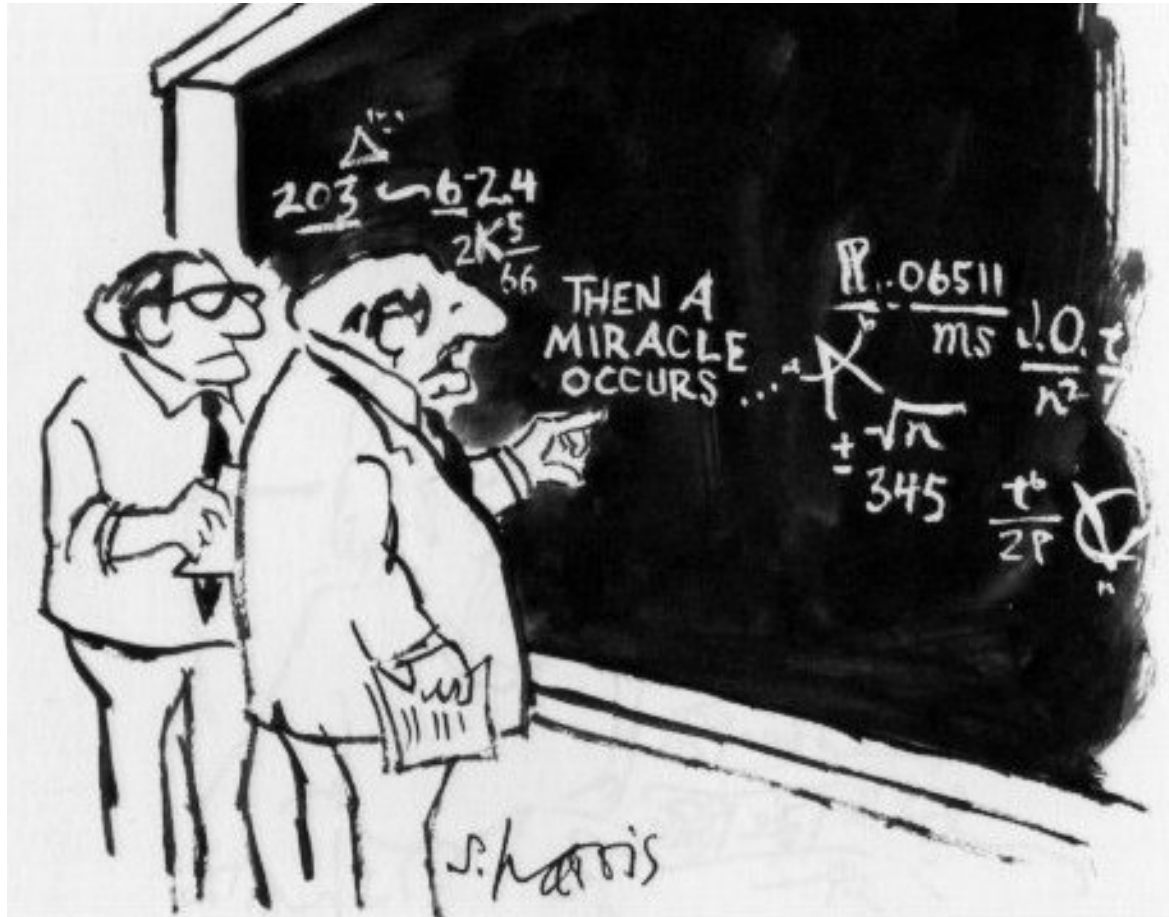
|         |          |
|---------|----------|
| Lat     | 11.7047  |
| Lon     | 48.2066  |
| Alt     | WAIT     |
| Hdg     | 173.19   |
| G'Vel   | WAIT     |
| AltMSL  | 1849.6   |
| G'Speed | 60.0974  |
| HDOP    | 0.9      |
| SATused | 10       |
| VDOP    | 1.5      |
| UTC     | 14:16:47 |



- most by static analysis (each developer & nightly runs)
  - removed all stupid bugs
  - identified under-specification
- few by system testing
  - masking defects during analysis
  - ignoring failed proofs
  - incomplete specification
- **one during operation**
  - faulty but non-crashing behavior
  - missed during system testing
  - unverified assumptions about sensor data (beyond code)

- Very little debugging work
  - Practically no exceptions during system testing
  - No issues with reproduction and isolation of failures
- SPARK tools work very well
  - Defect detection with almost no additional effort
  - Results are precise: `Mypack:9:35: overflow check might fail`
  - Effective multi-threading: separation of critical tasks
  - Verification automation as continuous integration with git
  - Verification of physical dimensions
  - Floats are difficult but possible
  - Verification of high-level behavior is difficult but possible

code released to open source: <https://github.com/tum-ei-rCS/StratoX>

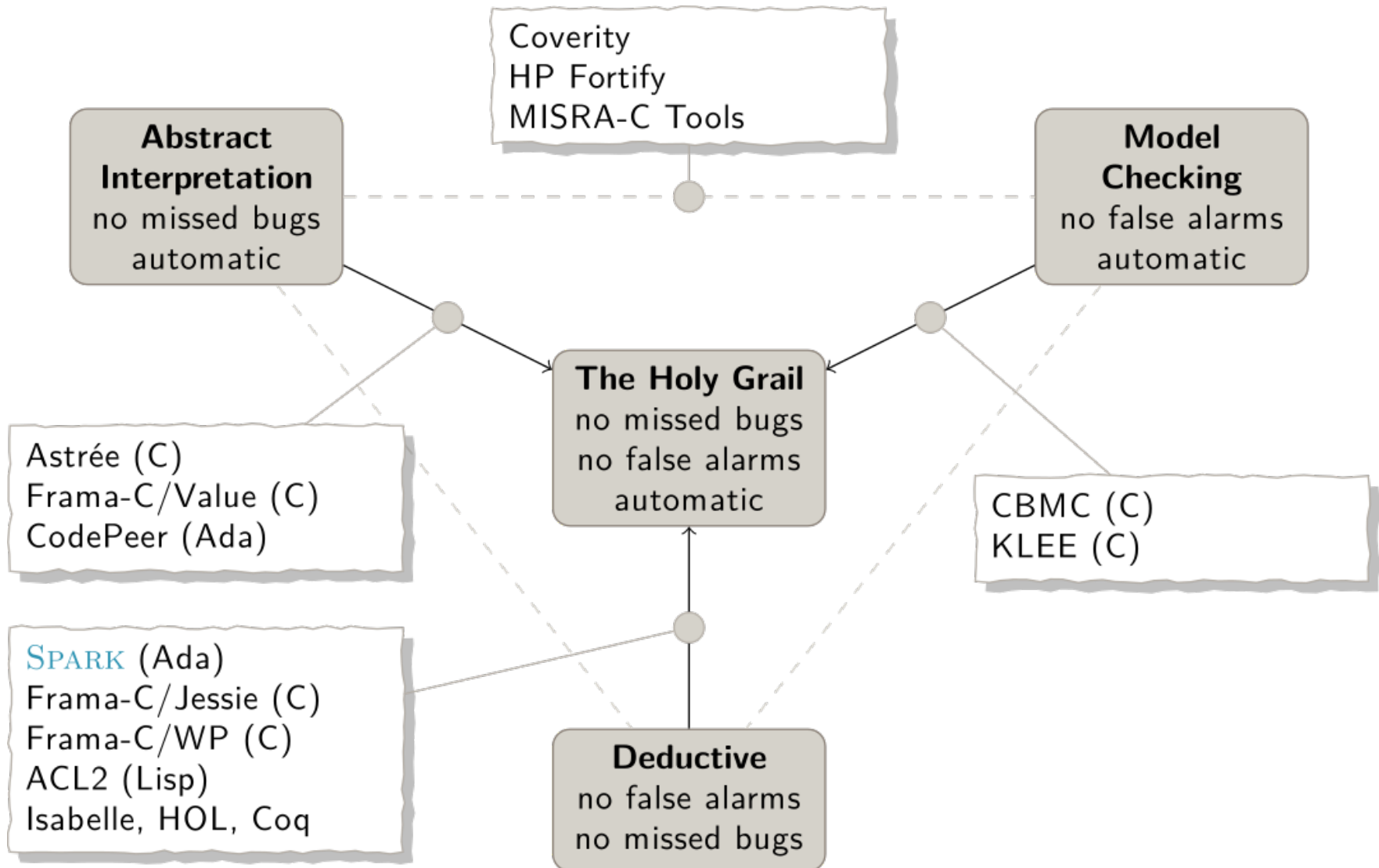


**“I think you should be more explicit here in step two.”**

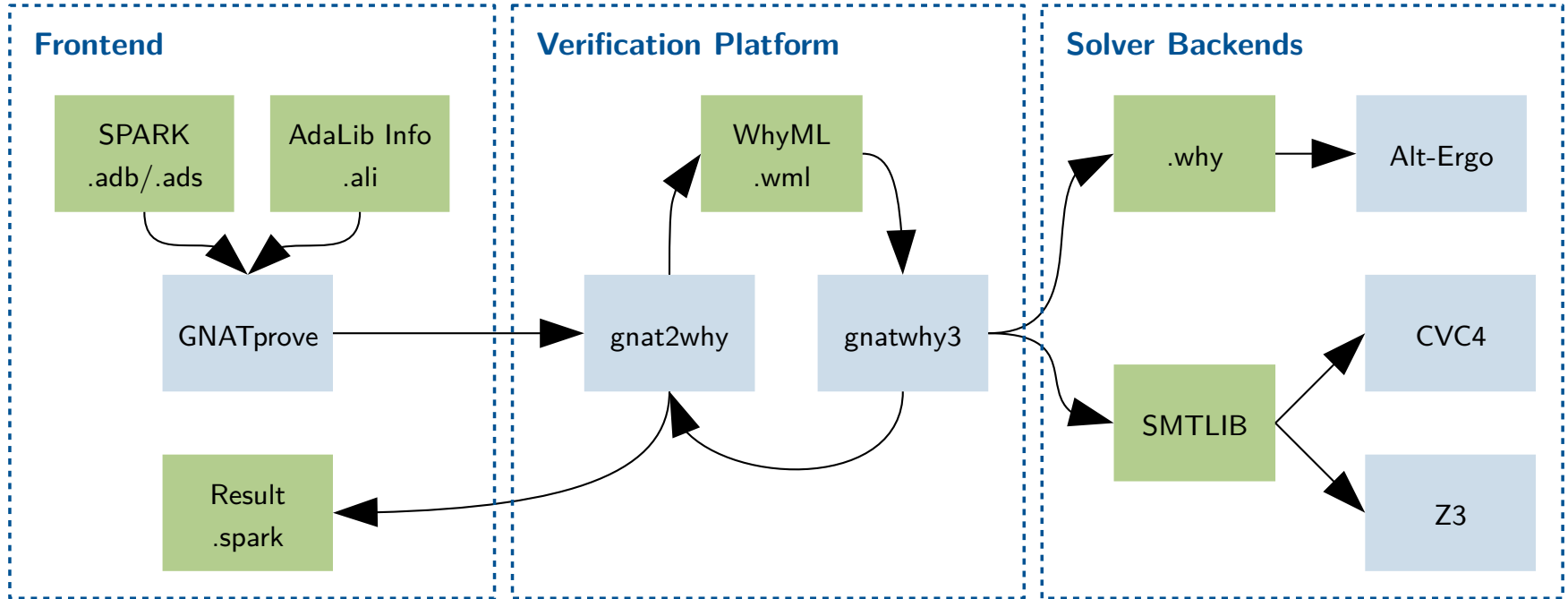
from *What's so Funny about Science?* by Sidney Harris (1977)

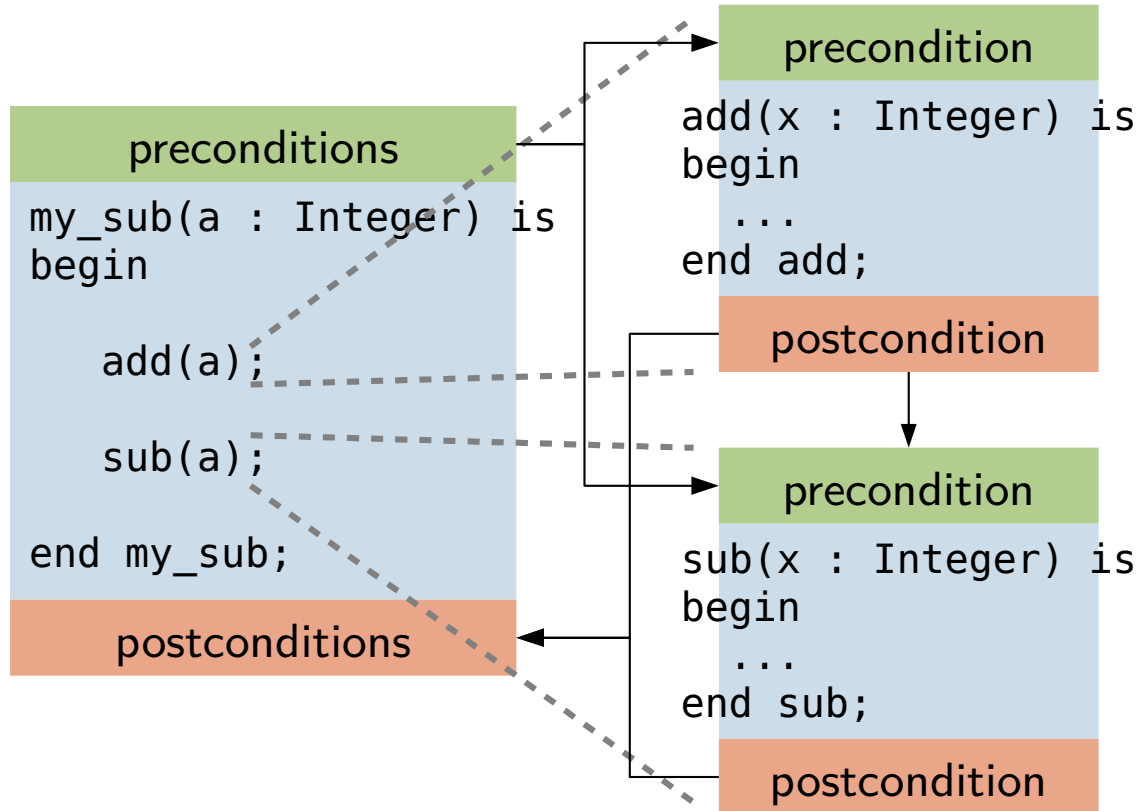
- M. Becker, E. Regnath, Samarjit Chakraborty “Development and Verification of a Flight Stack for a High-Altitude Glider in Ada/SPARK 2014”, In 36th International Conference on Computer Safety, Reliability and Security (SAFECOMP), Trento, IT.
- “Airworthiness directives; the boeing company airplanes”, Federal Aviation Administration, Tech. Rep. 2015-10066, May 1, 2015.
- Adacore, SPARK 2014 reference manual.
- Adacore, SPARK 2014 user guide, version 18.0.
- Ada reference manual, ISO/IEC Std. 8652, 2012



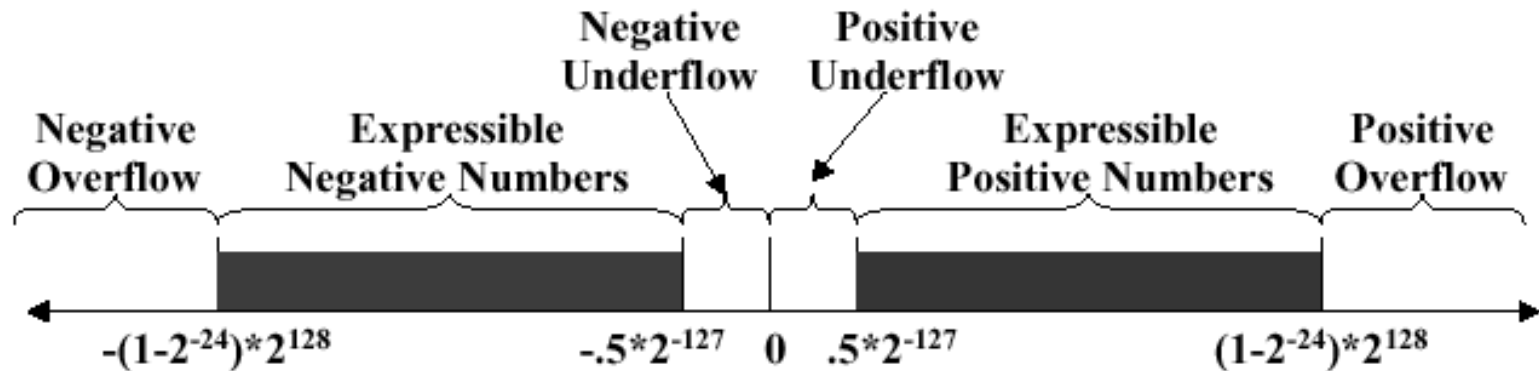


# GNATprove internal





```
1 -- Float Underflow
2 function Sin ( x : Float ) return Float with
3     Post => Sin'Result in -1.0 .. 1.0;           -- OK
4
5 pragma Assert ( ( Sin(x) )**2 in -1.0 .. 1.0 ); -- Might fail
```



# Final GNATprove Results

| <b>SPARK Analysis</b> | <b>Total</b> | <b>Flow</b> | <b>Interval</b> | <b>Proved</b> | <b>Justified</b> | <b>Unproven</b> |
|-----------------------|--------------|-------------|-----------------|---------------|------------------|-----------------|
| Data Dependencies     |              |             |                 |               |                  |                 |
| Flow Dependencies     |              |             |                 |               |                  |                 |
| Initialization        | 1540         | 1510        |                 |               | 29               | 1               |
| Non Aliasing          | 16           | 16          |                 |               |                  |                 |
| Run-Time Checks       | 1711         |             | 366             | 1117          | 4                | 224             |
| Assertions            | 15           |             |                 | 15            |                  |                 |
| Functional Contracts  | 282          |             |                 | 277           |                  | 5               |
| LSP Verification      |              |             |                 |               |                  |                 |
| <b>Total</b>          | <b>3564</b>  | <b>1526</b> | <b>366</b>      | <b>1409</b>   | <b>33</b>        | <b>230</b>      |

Subprogram Coverage : 538 / 1227 (43.8%) 538 / 654 (82%)

Proven Properties: 3334 / 3564 (93.5%)

Proven Run-Time Errors: 1487 / 1711 (86.9%)