

# Verification of Real-Time Specification Patterns on Time Transition Systems

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**Abstract.** We address the problem of checking properties of Time Transition Systems (TTS), a generalization of Time Petri Nets with data variables and priorities. We are specifically interested by time-related properties expressed using real-time specification patterns, a language inspired by properties commonly found during the analysis of reactive systems. Our verification approach is based on the use of observers in order to transform the verification of timed patterns into the verification of simpler LTL formulas. While the use of observers for model-checking timed extensions of temporal logics is fairly common, our approach is original in several ways. In addition to traditional observers based on the monitoring of places and transitions, we propose a new class of observers for TTS models based on the monitoring of data modifications that appears to be more efficient in practice. Moreover, we provide a formal framework to prove that observers are correct and non-intrusive, meaning that they do not affect the system under observation. Our approach has been integrated in a verification toolchain for Fiacre, a formal modeling language that can be compiled into TTS.

## 1 Introduction

A distinctive feature of real-time systems is to be subject to severe time constraints that arise from critical interactions between the system and its environment. Since reasoning about real-time systems is difficult, it is important to be able to apply formal validation techniques early during the development process and to define formally the requirements that need to be checked. In this work, we follow a classical approach for explicit-state model checking: we use a high-level language able to describe systems of communicating processes; our goal is to check the validity of specifications expressed in a logical-based formalism; the verification of a system consists in compiling its description and its requirements into a low-level model for which we have the appropriate theory and the convenient tooling.

We propose a new treatment for this traditional approach. We focus on a dense real-time model and use a patterns specification language instead of a timed extension of a temporal logic. One of our contribution is to propose a new decidable verification procedure for a real-time extension to the patterns language of Dwyer et al. [12]. Instead of using real-time extensions of temporal

logic, we propose a patterns language, inspired by properties commonly found during the analysis of reactive systems, that can facilitate the specification of requirements by non-expert. This patterns language can be used to express constraints on the timing as well as the order of events, such as the compliance to deadline or minimum time bounds on the delay between events. While we may rely on timed temporal logics as a way to define the semantics of patterns, the choice of a patterns language has some advantages. For one, we do not have to limit ourselves to a decidable fragment of a particular logic—which may be too restrictive—or have to pay the price of using a comprehensive real-time model-checking, that have a very high theoretical complexity.

We address the problem of checking patterns on Time Transition System (TTS), a generalization of Time Petri Nets with data variables and priorities. Our verification approach is based on the use of observers in order to transform the verification of timed patterns into the verification of simpler reachability properties. For the purpose of this work, we focus on a simple *deadline pattern*, named *leadsto*, and define different classes of observers that can be used to check it. We have applied our approach to a much richer patterns language, with operators that can express requirements on the occurrence and order of events in a system during its execution. A complete description of the patterns language can be found in [1] (we also include a global presentation of the patterns language in Appendix A).

While the use of observers for model-checking timed extensions of temporal logics is fairly common, our approach of the problem is original in several ways. In addition to traditional observers that monitor places and transitions, we propose a new class of observers for Time Transition System (TTS) models that monitor data modifications, and which appears to be more efficient in practice. Another contribution is the definition of a formal framework to prove that observers are correct and non-intrusive, meaning that they do not affect the system under observation. This framework is useful for adding new patterns in our language or for proving the soundness of optimizations.

Beside this theoretical framework, we also provide experimental results. The complete framework defined in this paper has been integrated into a verification toolchain for Fiacre [7]—the high-level modeling language, in our context (see Fig 1). Fiacre is the intermediate language used for model verification in Topcased [13]—an Eclipse based toolkit for critical systems—where it is used as the target of model transformation engines from various languages, such as SDL, UML or AADL [5]. Fiacre is also the source language of compilers into two verification toolboxes: TINA, the Time Petri Net Analyzer toolset [9], and CADP [14]. For the low-level model, we rely on Time Transition System (TTS), a generalization of Time Petri Nets with data variables and priorities that is one of the input formats accepted by TINA and the output of Frac compiler (the Fiacre compiler for the TINA toolbox). In our toolchain (Fig 1), the Fiacre program, which is combined with patterns, is compiled into TTS model using Frac compiler. The TTS generated is verified then with TINA toolbox. We give some experimental results on the impact of the choice of observers on the size

of the state graphs that need to be generated, that is on the space complexity of our verification method, and on time for verification which refers to the total time needed to generate and to verify the system.

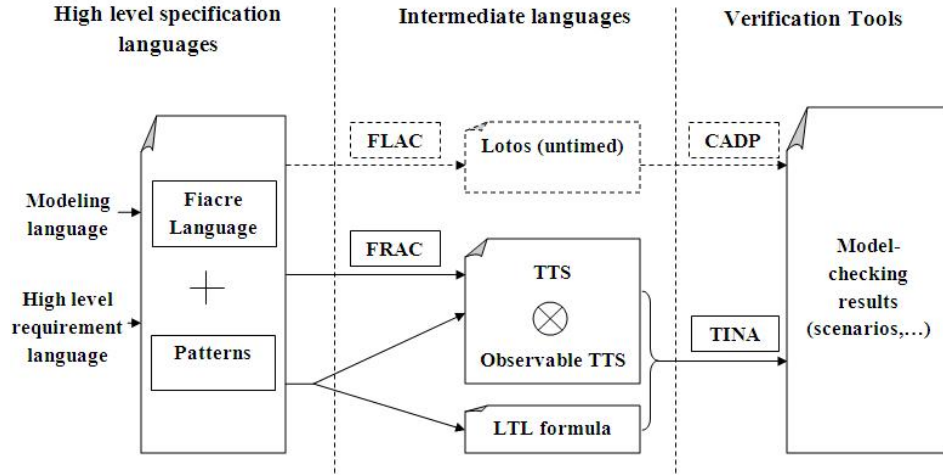


Fig. 1. The global verification toolchain

*Outline* we define the TTS model and the semantics of timed traces in Section 2. Sections 3 and 4 describe our property specification language and the verification framework. In Section 5, we give some experimental results on the use of the leadsto pattern. We conclude with a review of the related work, an outline of our contributions and some perspectives on future work.

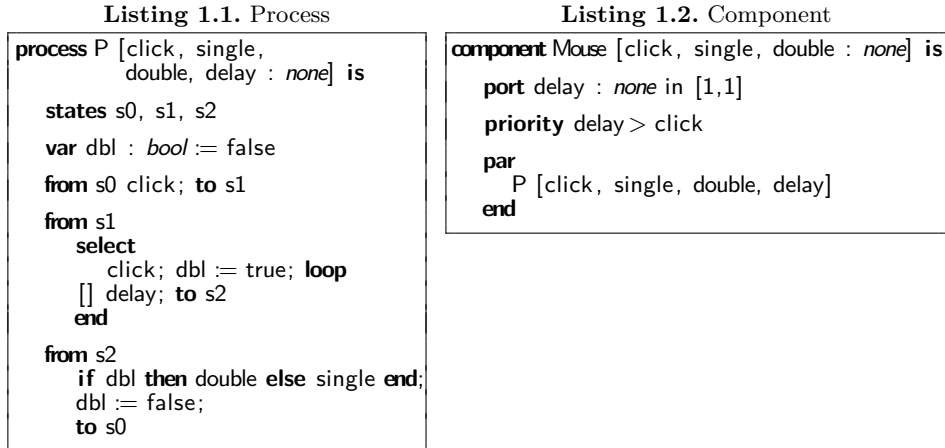
## 2 Time Transition Systems

We briefly describe the Fiacre formal verification language and show the connection between this high-level language and Time Transition Systems (TTS), an internal format used in our model-checking tools.

### 2.1 The Fiacre Language

Fiacre is a formal specification language designed to represent both the behavioral and timing aspects of real-time systems. The design of the language is inspired by Time Petri Nets (TPN) for its timing primitives, while the integration of time constraints and priorities into the language can be traced to the BIP framework [10]. A formal definition of the language is given in [7,8]. Fiacre programs are stratified in two main notions: *processes*, which are well-suited

for modeling structured activities, and *components*, which describes a system as a composition of processes, possibly in a hierarchical manner. The listings in Fig. 1.1 and 1.2 give a simple example that models the behavior of a mouse button with double-clicking. The behavior, in this case, is to emit the event *double* if there are more than two click events in *strictly less* than one unit of time (u.t.). Note that we use a dense-time model.



**Fig. 2.** A double-click example in Fiacre

A *process* is defined by a set of parameters and *control states*, each associated with a set of *complex transitions* (introduced by the keyword *from*). Complex transitions are expressions that declares how variables are updated and which transitions may fire. They are built from deterministic constructs available in classical programming languages (assignments, conditionals, sequential composition, ...); non-deterministic constructs (choice and non-deterministic assignments); communication events on ports; and jump to next state. For example, Listing 1.1 declares a process named P, with four communication ports (click to delay) and one local boolean variable, *dbl*. Ports may send and receive typed data. The port type *none* means that no data is exchanged, these ports simply act as synchronization events. Regarding complex transitions, the expression for *s1*, for instance, declares that in state *s1* the process may either: (1) receive a click event from the environment, set *dbl* to true and stay in state *s1*; or (2) receive an event *delay* and move to *s2*.

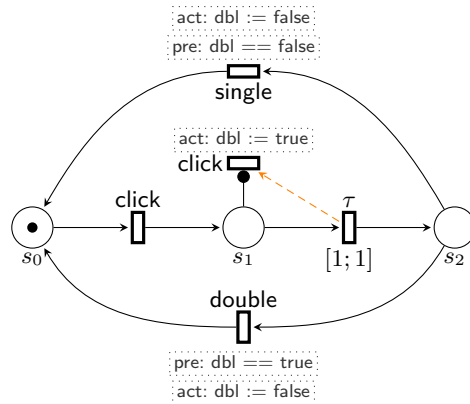
A *component* is defined as the parallel composition of processes and/or other components, expressed with the operator *par ... end*. In a composition, processes can interact both through synchronization (message-passing) and accesses to shared variables (shared memory). Components are the unit for process instantiation and for declaring ports and shared variables. The syntax of components allows to associate timing constraints with communications and to define priority

between communication events. The ability to express directly timing constraints in programs is a distinguishing feature of Fiacre. For example, in Listing 1.2, the declaration of the local port `delay` means that—for the instance of process `P` defined in `Mouse`—the transition from `s1` to `s2` should take exactly one unit of time.

We assume the reader is already familiar with the usual vocabulary of Time Petri nets [21] (such as the standard notions of markings and time intervals).

## 2.2 Informal Introduction

Time Transition Systems (TTS) are a generalization of Time Petri Nets (TPN) with priorities and data variables. This computational model is very close to the abstract model for real-time systems defined by Henzinger *et al* [18]—hence the choice of the name—with a different syntax; we use Petri Nets instead of product of automata. We introduce a graphical syntax for TTS using a simple example that models the behavior of a mouse button with double-clicking, as pictured in Fig. 3. The behavior, in this case, is to emit the event `double` if there are more than two click events in *strictly less* than one unit of time (u.t.). Its precise semantics, expressed in terms of *timed traces*, is defined further (2.4).



**Fig. 3.** The double-click example in TTS

Ignoring at first side conditions and side effects (the `pre` and `act` expressions inside dotted rectangles), the TTS in Fig. 3 can be viewed as a TPN with one token in place  $s_0$  as its initial marking. From this “state”, a `click` transition may occur and move the token from  $s_0$  to  $s_1$ . With this marking, the internal transition  $\tau$  is enabled and will fire after exactly one unit of time, since the token in  $s_1$  is not consumed by any other transition. Meanwhile, the transition labeled `click` may be fired one or more times without removing the token from  $s_1$ , as indicated by the *read arc* (arcs ending with a black dot). After exactly one unit

of time, because of the priority arc (a dashed arrow between transitions), the click transition is disabled until the token moves from  $s_1$  to  $s_2$ .

Data is managed within the **act** and **pre** expressions that may be associated to each transition. These expressions may refer to a fixed set of variables that form the *store* of the TTS. Assume  $t$  is a transition with guards  $\mathbf{act}_t$  and  $\mathbf{pre}_t$ . In comparison with a TPN, a transition  $t$  in a TTS is enabled if there is both: (1) enough tokens in the places of its pre-condition; and (2) the predicate  $\mathbf{pre}_t$  is true. With respect to the firing of  $t$ , the main difference is that we modify the store by executing the action guard  $\mathbf{act}_t$ . For example, when the token reaches the place  $s_2$  in the TTS of Fig. 3, we use the value of **dbl** to test whether we should signal a double click or not.

### 2.3 Formal Definition

Notation : we write  $\mathbb{R}^+$  the set of nonnegative real numbers, and  $\mathcal{I}(\mathbb{R}^+)$  the set of non-empty convex subsets of  $\mathbb{R}^+$  (that is, intervals of  $\mathbb{R}^+$ , including all open or closed variants, as well as infinite intervals). Given an element  $I$  of  $\mathcal{I}(\mathbb{R}^+)$  and an element  $\delta$  of  $\mathbb{R}^+$ , we define  $I - \delta$  as the set  $\{x \in \mathbb{R}^+ \mid x + \delta \in I\}$ . If  $I - \delta$  is not empty, it is itself an element of  $\mathcal{I}(\mathbb{R}^+)$ .

**Definition 1 (Time Transition System).** *A TTS is a 9-tuple  $\langle P, T, S, \mathcal{M}, <, tc, enb, cfl, ac \rangle$ , and its state is a triple  $(m, s, dtc)$  where:*

- (a)  $P$ ,  $T$ , and  $S$  are three disjoint sets, of places, transitions, and stores, respectively.
- (b)  $\mathcal{M}$  is the set of markings of the TTS, that is, mappings from  $P$  to  $\{0, 1\}$ .
- (c)  $<$  is a binary, transitive relation over  $T$  which encodes the (static) priority relation between transitions.
- (d)  $tc$  (static time constraint) is a mapping from  $T$  to  $\mathcal{I}(\mathbb{R}^+)$ .
- (e)  $enb$  (enable predicate) is a predicate over  $T \times \mathcal{M} \times S$ ;  $cfl$  (conflict predicate) is a predicate over  $T \times \mathcal{M} \times T$  and  $ac$  (action) is a mapping from  $T \times \mathcal{M} \times S$  to  $\mathcal{M} \times S$ .
- (f) The TTS state  $(m, s, dtc)$  is an element of  $\mathcal{M} \times S \times (\mathcal{I}(\mathbb{R}^+))^T$ .  $dtc$  is a mapping called the dynamic time constraint.

The initial state of a TTS is written  $(m^{init}, s^{init}, tc)$ . It requires the dynamic time constraint of every transition to be equal to its static time constraint.

We make some comments on this definition. Condition (b) implies that the underlying Petri Net is one-safe. The interval  $dtc(t)$  is used to record the time elapsed waiting for the firing of  $t$ ; therefore we require  $tc(t) = dtc(t)$  to hold in the initial state for all transitions  $t$  in  $T$ . In Fig.3, transitions without time constraints are associated to the time interval  $[0, +\infty[$ . In condition (e), the predicate  $enb(t, m, s)$  indicates whether  $t$  is enabled under marking  $m$  and store  $s$ ;  $cfl(t_1, m, t_2)$  indicates whether firing  $t_1$  under marking  $m$  should reset the dynamic time interval of  $t_2$  to its default value  $tc(t_2)$ ; and  $ac(t, m, s)$  returns a

new marking  $m'$  and a new store  $s'$  corresponding to the effect of firing  $t$  under marking  $m$  and store  $s$ .

It is easy to show that the TTS model includes Time Petri Nets: take an empty store and define  $\text{enb}(t, m, \emptyset)$  as the predicate  $m \geq \text{pre}(t)$ ,  $\text{cfl}(t, m, t')$  as the predicate  $m - \text{pre}(t) < \text{pre}(t')$  and  $\text{ac}(t, m, \emptyset)$  as the function  $m - \text{pre}(t) + \text{post}(t)$ .

## 2.4 Semantics of TTS expressed as Timed Traces

The behavior of a TTS is abstracted as a set of traces, called timed traces. In contrast, the behavior expected by the user is expressed with some properties (some invariants) to be checked against this set of timed traces. For instance, one may check the invariant that variable `dbl` is never true when  $s_0$  is marked (using an accessibility check), or that transition `click` is followed by either `single` or `double` within one time unit (using an observer, as described in Sec. 3). As a consequence, traces must contain information about fired transitions (e.g. `single`), markings (e.g.  $m(s_0)$ ), store (e.g. current value of `dbl`), and elapsing of time (e.g. to detect the one-time-unit deadline).

Formally, we define an event  $\omega$  as a triple  $(t, m, s)$  recording the marking and store immediately after the transition  $t$  has been fired. We denote  $\Omega$  the set  $T \times \mathcal{M} \times S$  of possible events.

**Definition 2 (Timed trace).** *A timed trace  $\sigma$  is a possibly infinite sequence of events  $\omega \in \Omega$  and durations  $d(\delta)$  with  $\delta \in \mathbb{R}^+$ . Formally,  $\sigma$  is a partial mapping from  $\mathbb{N}$  to  $\Omega^* = \Omega \cup \{d(\delta) \mid \delta \in \mathbb{R}^+\}$  such that  $\sigma(i)$  is defined whenever  $\sigma(j)$  is defined and  $i \leq j$ . The domain of  $\sigma$  is written  $\text{dom } \sigma$ .*

Using classic notations for sequences, the empty sequence is denoted  $\epsilon$ ; given a finite sequence  $\sigma$  and a—possibly infinite—sequence  $\sigma'$ , we denote  $\sigma\sigma'$  the concatenation of  $\sigma$  and  $\sigma'$ . Concatenation is associative.

**Definition 3 (Duration).** *Given a finite trace  $\sigma$ , we define its duration,  $\Delta(\sigma)$ , using the following inductive rules:*

$$\Delta(\epsilon) = 0 \qquad \Delta(\sigma.d(\delta)) = \Delta(\sigma) + \delta \qquad \Delta(\sigma.\omega) = \Delta(\sigma)$$

*We extend  $\Delta$  to infinite traces, by defining  $\Delta(\sigma)$  as the limit of  $\Delta(\sigma_i)$  where  $\sigma_i$  are growing prefixes of  $\sigma$ .*

Infinite traces are expected to have an infinite duration. Indeed, to rule out Zeno behaviors, we only consider traces that let time elapse. Hence, the following definition:

**Definition 4 (Well-formed traces).** *A trace  $\sigma$  is well-formed if and only if  $\text{dom}(\sigma)$  is finite or  $\Delta(\sigma) = \infty$ .*

The following definition provides an equivalence relation over timed traces. This relation guarantees that a well-formed trace (not exhibiting a Zeno behavior) is only equivalent to well-formed traces. One way to achieve this would

be to require that two equivalent traces may only differ by a finite number of differences. However, we also want to consider equivalent some traces that have an infinite number of differences, such as for example the infinite traces  $(d(1).d(1).\omega)^*$  and  $(d(2).\omega)^*$  (where  $X^*$  is the infinite repetition of  $X$ ). Our solution is to require that, within a finite time interval  $[0, \delta]$ , equivalent traces must contain a finite number of differences.

**Definition 5 (Equivalence over timed traces).** *For each  $\delta > 0$ , we define  $\equiv_\delta$  as the smallest equivalence relation over timed traces satisfying  $\sigma.d(0).\sigma' \equiv_\delta \sigma.\sigma'$ ,  $\sigma.d(\delta_1).d(\delta_2).\sigma' \equiv \sigma.d(\delta_1 + \delta_2).\sigma'$ , and  $\sigma.\sigma' \equiv_\delta \sigma.\sigma''$  whenever  $\Delta(\sigma) > \delta$ . The relation  $\equiv$  is the intersection of  $\equiv_\delta$  for all  $\delta > 0$ .*

By construction,  $\equiv$  is an equivalence relation. Moreover,  $\sigma_1 \equiv \sigma_2$  implies  $\Delta(\sigma_1) = \Delta(\sigma_2)$ . Our notion of timed trace is quite expressive. In particular, we are able to describe events which happen at the same date (with no delay in between) while keeping a causality relation (one event is before another).

We now consider briefly the dynamic semantics of TTS, which is similar to the semantics of Time Petri-Nets [21]. It is expressed as a binary relation between states labeled by elements of  $\Omega^*$ , and written  $(m, s, \text{dte}) \xrightarrow{l} (m', s', \text{dte}')$ , where  $l$  is either a delay  $d(\delta)$  with  $\delta \in \mathbb{R}^+$  or an event  $\omega \in \Omega$ . We say that transition  $t$  is *enabled* if  $\text{enb}(t, m, s)$  is true. A transition  $t$  is *fireable* if it is enabled, *time-enabled* (that is  $0 \in \text{dte}(t)$ ) and there is no fireable transition  $t'$  that has priority over  $t$  (that is  $t < t'$ ). Given these definitions, a TTS with state  $(m, s, \text{dte})$  may progress in two ways:

- *Time elapses* by an amount  $\delta$  in  $\mathbb{R}^+$ , provided  $\delta \in \text{dte}(t)$  for all enabled transitions, meaning that no transition  $t$  is urgent. In that case, we define  $\text{dte}'$  by  $\text{dte}'(t) = \text{dte}(t) - \delta$  for all enabled transitions  $t$  and  $\text{dte}'(t) = \text{te}(t)$  for disabled transitions. Under these hypotheses, we have

$$(m, s, \text{dte}) \xrightarrow{d(\delta)} (m, s, \text{dte}')$$

- *A fireable transition  $t$  fires.* Let  $(m', \sigma')$  be  $\text{ac}(t, m, s)$ , and  $\text{dte}'$  be a new mapping such that  $\text{dte}'(t') = \text{te}(t')$  for all newly enabled transitions  $t'$  and for all transitions  $t'$  in conflict with  $t$  (such that  $\text{cfl}(t, m, t')$  holds). For other transitions, we define  $\text{dte}'(t') = \text{dte}(t')$ . Under these hypotheses, we have

$$(m, s, \text{dte}) \xrightarrow{(t, m', \sigma')} (m', s', \text{dte}')$$

We inductively define  $\xrightarrow{\sigma}$ , where  $\sigma$  is a finite trace:  $\xrightarrow{\epsilon}$  is defined as the identity relation over states, and  $\xrightarrow{\sigma\omega}$  is defined as the composition of  $\xrightarrow{\sigma}$  and  $\xrightarrow{\omega}$  (we omit details). We write  $(m, s, \text{dte}) \xrightarrow{\sigma}$  whenever there exist a state  $(m', s', \text{dte}')$  such that  $(m, s, \text{dte}) \xrightarrow{\sigma} (m', s', \text{dte}')$ . Given an infinite trace  $\sigma$ , we write  $(m, s, \text{dte}) \xrightarrow{\sigma}$  if and only if  $(m, s, \text{dte}) \xrightarrow{\sigma'}$  holds for all  $\sigma'$  finite prefixes of  $\sigma$ . Finally, the set of traces of a TTS  $N$  is the set of well-formed traces  $\sigma$  such that  $(m^{\text{init}}, s^{\text{init}}, \text{te}) \xrightarrow{\sigma}$  holds. This set is written  $\Sigma(N)$ .

The TINA verification toolbox [9] offers several tools to work with TTS files, including a model-checker for a State-Event version of LTL. However, a



strong limitation of LTL model-checking is that it does not allow the user to express timing constraints, for example, that some deadline between significant events is met. In Sect. 4, we introduce a specification language that makes it easier to express real-time requirements. Each pattern in this language can be compiled into an observer expressed as a TTS, which is then composed with the original system, using a composition operator defined next. Thus, we reduce the verification of timed patterns into the verification of simple LTL properties on the composed system, for which we have the adequate tooling.

## 2.5 Composition of TTS and Composition of Traces

We study the composition of two TTS and consider the relation between traces of the composed system and traces of its components. This operation is particularly significant in the context of this work, since both the system and the observer are TTS and we use composition to graft the latter to the former. In particular, we are interested in conditions ensuring that the behavior of the observer does not interfere with the behavior of the observed system.

The composition of two TTS is basically the same as for TPN: we assume given a function `lab` associating a label, taken in a countable set  $\mathcal{L}$ , to every transition. Then, transitions bearing the same label are synchronized. However, some conditions must be ensured so that composition is sound, as defined next:

**Definition 6 (Composable TTS, synchronized transitions).** *We consider two TTS, namely  $N_1$  and  $N_2$ , defined as  $\langle P_i, T_i, S_i, \mathcal{M}_i, <_i, tc_i, enb_i, cfl_i, ac_i \rangle$  for  $i=1,2$ , respectively. The set of synchronized transitions of  $N_1$  is  $\{t_1 \in T_1 \mid \exists t_2 \in T_2 . \text{lab}(t_1) = \text{lab}(t_2)\}$ . We define the set of synchronized transitions of  $N_2$  similarly. Then,  $N_1$  and  $N_2$  are composable if the following conditions hold:*

1.  $P_1 \cup T_1 \cup S_1$  is disjoint from  $P_2 \cup T_2 \cup S_2$ .
2. for  $i = 1, 2$ , every synchronized transition  $t_i$  of  $N_i$  is such that  $tc_i(t_i) = [0, +\infty[$ , and there is no transition  $t' \in T_i$  with  $t' < t_i$ .

The first condition ensures that  $N_1$  and  $N_2$  are disjoint, in particular they must use disjoint stores. As a consequence, no information can be exchanged through shared variables. Thus, synchronization occurs through transitions only. As stated by the second condition, in every pair of synchronized transitions, both transitions must have a trivial time constraint  $[0, +\infty[$ . This condition as well as the condition on priorities is necessary to ensure compositionality, as stated by Property 1 below.

**Definition 7 (Composition).** *Assuming  $N_1$  and  $N_2$  are defined as above, let  $N$  be the TTS corresponding to their composition, which we write  $N = N_1 \otimes N_2$ . It is defined by the 9-tuple  $\langle P, T, S, \mathcal{M}, <, tc, enb, cfl, ac \rangle$  where:*

1.  $P = P_1 \cup P_2$

2. Let  $\perp$  be an element not in  $T_1 \cup T_2$ . Let  $T_1^\perp$  be  $T_1 \cup \{\perp\}$  and  $T_2^\perp$  be  $T_2 \cup \{\perp\}$ . We define  $T$  as the following subset of  $T_1^\perp \times T_2^\perp$ :
 
$$T = \{(t_1, t_2) \mid t_1 \in T_1, t_2 \in T_2, \text{lab}(t_1) = \text{lab}(t_2)\} \\ \cup \{(t_1, \perp) \mid t_1 \in T_1 \text{ and } t_1 \text{ is not synchronized}\} \\ \cup \{(\perp, t_2) \mid t_2 \in T_2 \text{ and } t_2 \text{ is not synchronized}\}$$
 We remark that  $(\perp, \perp) \notin T$ .
3.  $S = S_1 \times S_2$
4.  $\mathcal{M} = \{0, 1\}^P$ . By noticing that  $\mathcal{M}$  is in bijection with  $\mathcal{M}_1 \times \mathcal{M}_2$ , we may freely consider that elements of  $\mathcal{M}$  are of the form  $(m_1, m_2)$  with  $m_1 \in \mathcal{M}_1$  and  $m_2 \in \mathcal{M}_2$ .
5.  $<_1$  is a binary relation on  $T_1$ . We may freely consider it as a binary relation on  $T_1^\perp$  (and so there is no  $t \in T_1^\perp$  with  $t < \perp$  or  $\perp < t$ ). Similarly,  $<_2$  is considered as a binary relation on  $T_2^\perp$ . Then,  $<$  is defined by: for all  $(t_1, t'_1, t_2, t'_2) \in (T_1^\perp)^2 \times (T_2^\perp)^2$ , we have  $(t_1, t_2) < (t'_1, t'_2)$  if and only if  $t_1 < t'_1$  or  $t_2 < t'_2$ . As required,  $<$  is transitive (we omit the proof).
6. For all  $(t_1, t_2)$  in  $T$ , we define  $\text{tc}(t_1, t_2)$  as  $\text{tc}_1(t_1)$  if  $t_1 \neq \perp$ , and as  $\text{tc}_2(t_2)$  otherwise.
7.  $\text{enb}((t_1, t_2), (m_1, m_2), (s_1, s_2))$  is defined as  $(t_1 = \perp \vee \text{enb}_1(t_1, m_1, s_1)) \wedge (t_2 = \perp \vee \text{enb}_2(t_2, m_2, s_2))$ .
8.  $\text{cfl}((t_1, t_2), (m_1, m_2), (t'_1, t'_2))$  is defined as  $(t_1 \neq \perp \wedge t'_1 \neq \perp \wedge \text{cfl}_1(t_1, m_1, t'_1)) \vee (t_2 \neq \perp \wedge t'_2 \neq \perp \wedge \text{cfl}_2(t_2, m_2, t'_2))$
9. By convention, for  $i = 1, 2$ , and for any  $m$  and  $s$ , we define  $\text{ac}_i(\perp, m, s)$  as  $(m, s)$ . Then,  $\text{ac}((t_1, t_2), (m_1, m_2), (s_1, s_2))$  is defined as the pair  $((m'_1, m'_2), (s'_1, s'_2))$ , where  $(m'_1, s'_1)$  is  $\text{ac}_1(t_1, m_1, s_1)$  and  $(m'_2, s'_2)$  is  $\text{ac}_2(t_2, m_2, s_2)$ .

Additionally, the initial state is defined as  $((m_1^{\text{init}}, m_2^{\text{init}}), (s_1^{\text{init}}, s_2^{\text{init}}), \text{tc})$ .

We now define composition of traces, and then show, in Property 1, that traces generated by  $N$  correspond to composition of traces from  $N_1$  and traces from  $N_2$ .

We extend  $\text{lab}$  to events and duration by defining  $\text{lab}(t, m, \sigma) = \text{lab}(t)$  and  $\text{lab}(d(\delta)) = d(\delta)$ . Additionally, we say that an event  $\omega$  is synchronized if and only if  $\omega$  is a delay  $d(\delta)$  or  $\omega$  is  $(t, m, \sigma)$  and  $t$  is synchronized (as defined in Def. 6).

In the same way that systems can be composed, it is possible to compose a timed trace of a TTS  $N_1$  with the trace of another TTS  $N_2$  when some conditions are met. Basically, events with the same label must occur synchronously, time elapses synchronously in both systems, and unsynchronized events—events that are not shared between  $N_1$  and  $N_2$ —can only be composed with  $d(0)$  (meaning they are not synchronized with an observable event).

**Definition 8 (Composable traces).** Let  $\Omega_1$  and  $\Omega_2$  be the set of events of two TTS  $N_1$  and  $N_2$ , respectively. We define the relation  $\bowtie$  between  $\Omega_1^*$  and  $\Omega_2^*$  as the smallest relation satisfying the following inference system:

$$\frac{\text{lab}(\omega_1) = \text{lab}(\omega_2)}{\omega_1 \bowtie \omega_2} \quad \frac{\omega_2 \text{ not synchronized}}{d(0) \bowtie \omega_2} \quad \frac{\omega_1 \text{ not synchronized}}{\omega_1 \bowtie d(0)}$$

This relation can be extended to pairs of traces  $(\sigma_1, \sigma_2)$  of  $N_1 \times N_2$  as follows. We say that  $\sigma_1$  and  $\sigma_2$  are composable, which we write  $\sigma_1 \bowtie \sigma_2$ , if and only if  $\text{dom } \sigma_1 = \text{dom } \sigma_2$  and  $\sigma_1(i) \bowtie \sigma_2(i)$  holds for all  $i \in \text{dom } \sigma_1$ . Notice that  $\sigma_1 \bowtie \sigma_2$  implies  $\Delta(\sigma_1) = \Delta(\sigma_2)$ .

We are now able to state the compositionality property. Remind that  $\Sigma(N)$  is the set of traces of  $N$ .

*Property 1 (Compositionality).* Assume  $N_1$  and  $N_2$  are composable systems with events in  $\Omega_1$  and  $\Omega_2$  respectively. Let  $N$  be  $N_1 \otimes N_2$ ; we write  $\Omega$  its set of events. Then there exists a bijection  $f$  between  $\Omega$  and a subset of  $\Omega_1^* \times \Omega_2^*$  such that:  $\sigma \in \Sigma(N_1 \otimes N_2)$  if and only if there exists a pair of traces  $(\sigma_1, \sigma_2)$  of  $\Sigma(N_1) \times \Sigma(N_2)$  with  $\sigma_1 \bowtie \sigma_2$ ,  $\text{dom } \sigma = \text{dom } \sigma_1$ , and  $\forall i \in \text{dom } \sigma \begin{cases} \sigma(i) = d(\delta) & \text{if } \sigma_1(i) = \sigma_2(i) = d(\delta) \\ \sigma(i) = f^{-1}(\sigma_1(i), \sigma_2(i)) & \text{otherwise} \end{cases}$ .

In other words, given a trace  $\sigma \in \Sigma(N)$ , one may extract two composable traces  $\sigma_1 \in \Sigma(N_1)$  and  $\sigma_2 \in \Sigma(N_2)$ . Conversely, given two composable traces  $\sigma_1 \in \Sigma(N_1)$  and  $\sigma_2 \in \Sigma(N_2)$ , one may build a corresponding trace in  $\Sigma(N)$ , which we will write  $\sigma_1 \otimes \sigma_2$ . Thus, this property characterizes the set of traces of  $N$  in terms of traces of  $N_1$  and  $N_2$ .

*Proof.* Let  $E$  be the set  $(\Omega_1 \cup \{d(0)\}) \times (\Omega_2 \cup \{d(0)\}) \setminus (d(0), d(0))$ . Let  $f$  be the bijection between  $\Omega$  and  $E$  defined as

- if  $t_1 \neq \perp \wedge t_2 \neq \perp$ , then  $f((t_1, t_2), (m_1, m_2), (s_1, s_2))$  is  $((t_1, m_1, s_1), (t_2, m_2, s_2))$ .
- if  $t_1 \neq \perp$ , then  $f((t_1, \perp), (m_1, m_2), (s_1, s_2))$  is  $((t_1, m_1, s_1), d(0))$ .
- if  $t_2 \neq \perp$ , then  $f((\perp, t_2), (m_1, m_2), (s_1, s_2))$  is  $(d(0), (t_2, m_2, s_2))$ .

We now show that  $f$  satisfies the given property. We prove each way of the equivalence independently.

Assume  $\sigma$  is a trace of  $N$ . Let us define  $\sigma_1$  and  $\sigma_2$  by  $\text{dom } \sigma_1 = \text{dom } \sigma_2 = \text{dom } \sigma$  and for all  $i \in \text{dom } \sigma$ , if  $\sigma(i)$  is  $d(\delta)$  (for some  $\delta$ ), then  $\sigma_1(i) = \sigma_2(i) = d(\delta)$ , otherwise  $\sigma(i)$  is an event  $\omega$ , then let  $(\sigma_1(i), \sigma_2(i))$  be  $f(\omega)$ . It is straightforward to check that  $\sigma_1 \bowtie \sigma_2$  holds. It remains to be shown that  $\sigma_1$  (resp.  $\sigma_2$ ) is a trace of  $N_1$  (resp.  $N_2$ ). We show only the result for  $\sigma_1$ , the proof for  $\sigma_2$  being similar. This is a consequence of the two following implications, where  $\text{dte}_1$  is the function  $\text{dte}$  restricted to the domain  $T_1$  (and similarly for  $\text{dte}'_1$ ), and where  $f_1(\omega)$  is the first projection of  $f(\omega)$ . To ease the reading, we display these implications as inference rules:

$$\frac{((m_1, m_2), (s_1, s_2), \text{dte}) \xrightarrow{d(\delta)} ((m_1, m_2), (s_1, s_2), \text{dte}'_1)}{(m_1, s_1, \text{dte}_1) \xrightarrow{d(\delta)} (m_1, s_1, \text{dte}'_1)}$$

$$\frac{((m_1, m_2), (s_1, s_2), \text{dte}) \xrightarrow{\omega} ((m'_1, m'_2), (s'_1, s'_2), \text{dte}'_1)}{(m_1, s_1, \text{dte}_1) \xrightarrow{f_1(\omega)} (m'_1, s'_1, \text{dte}'_1)}$$

We only sketch the proof of these rules. The delicate part concerns  $\mathbf{dtc}$  (dealing with  $m$  and  $s$  is straightforward, by applying the definition of composition). More precisely, the (first projection of) enabled transitions of  $N$  is only a subset of enabled transitions of  $N_1$ , as a consequence of the definition of  $\mathbf{enb}$  in Def. 7. To state it otherwise, not all enabled transitions of  $N_1$  are enabled in  $N$ . Thus, there may be transitions  $t \in T_1$  such that  $\mathbf{dtc}'_1(t_1) = \mathbf{dtc}(t_1)$  whereas the expected value (according to the semantics of  $N_1$ ) would be  $\mathbf{dtc}'_1(t_1) - \delta$  (in the first rule) or  $\mathbf{tc}_1(t_1)$  (in the second rule). Fortunately, these transitions  $t_1$  must be synchronized transition (as a consequence of the definition of  $\mathbf{enb}$ ), therefore their time interval is always unconstrained, that is  $\mathbf{tc}_1(t_1) = \mathbf{dtc}_1(t_1) = [0; +\infty[$ , as required by Def. 6, and by remarking that  $[0; +\infty[-\delta = [0; +\infty[$  for any  $\delta$  in  $\mathbb{R}^+$ . Additionally, in the second rule, if  $f_1(\omega)$  is  $(t_1, m_1, s_1)$ , we must ensure that no other transition in  $N_1$  has priority over  $t_1$ , so that  $t_1$  is fireable. This is a consequence of the definition of priorities in Def. 7 and of the condition on priorities in Def.6.

Conversely, we assume given two composable traces  $\sigma_1$  and  $\sigma_2$  of  $N_1$  and  $N_2$ , respectively. The trace  $\sigma$  is defined as stated in the property. It remains to be shown that  $\sigma$  is indeed a trace of  $N$ . The proof is actually very similar to the previous case (with the small difference that the condition on priorities is not used).

This result is used to show the innocuousness of observers in Sec. 4.2.

### 3 A Real-Time Specification Patterns Language

We introduce the specification patterns language available in our framework. A global presentation of the patterns is given in Appendix A. More details about this language are given in [1]. In this paper, we focus on an observer-based approach for the verification of patterns over TTS models. We also follow a pragmatic approach for studying several possible implementations for observers—and selecting the most sensible one—which we believe is new. Our language extends the property specification patterns of Dwyer et al. [12] with the ability to express time delays between the occurrences of transitions. The framework is expressive enough to define properties like the compliance to deadlines, bounds on the worst-case execution time, etc. The advantage of proposing predefined patterns is to provide a simple formalism to non-experts for expressing properties that can be directly checked with our model-checking tools.

The patterns language follows the classification introduced in [12], with patterns arranged in categories such as universality, bounded existence, etc. In the following, we give some examples of *absence* and *response* patterns. More precisely, we focus on the “response pattern with delay” to show how patterns can be formally defined and to explain our different classes of observers.

**Absence pattern with delay** this category of patterns can be used to specify delays within which activities must not occur. A typical pattern in this category

can be used to assert that a transition labeled with say  $E_2$ , cannot occur between  $d_1$  and  $d_2$  units of time after the first occurrence of a transition labeled with  $E_1$ . This is expressed as follows in our language:

$$\mathbf{absent} \ E_2 \ \mathbf{after} \ E_1 \ \mathbf{for} \ \mathbf{interval} \ [d_1; d_2] \ . \quad (\mathbf{absent})$$

An example of use for this pattern would be an (unsatisfied) requirement that we cannot have two double clicks in less than 2 units of time (u.t.), that is **absent double after double for interval** [0; 2]. A more contrived example consists in requiring that if there are no single clicks in the first 10 u.t. of an execution then there should be no double clicks at all. This requirement can be expressed using the composition of two absence patterns using the implication operator and the reserved transition init (that identifies the start of the system):

$$\begin{aligned} & (\mathbf{absent} \ \mathbf{single} \ \mathbf{after} \ \mathbf{init} \ \mathbf{for} \ \mathbf{interval} \ [0; 10]) \\ & \Rightarrow (\mathbf{absent} \ \mathbf{double} \ \mathbf{after} \ \mathbf{init} \ \mathbf{for} \ \mathbf{interval} \ [0; \infty]) \ . \end{aligned}$$

**Response pattern with delay** this category of patterns can be used to express delays between transitions. The typical example of response pattern states that every occurrence of a transition labeled with  $E_1$  must be followed by an occurrence of a transition labeled with  $E_2$  within a time interval  $I$ . (We consider the first occurrence of  $E_2$  after  $E_1$ .)

$$E_1 \ \mathbf{leadsto} \ E_2 \ \mathbf{within} \ I \ . \quad (\mathbf{leadsto})$$

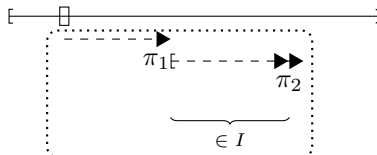
For example, using a disjunction of patterns, we can bound the time between a click and a mouse event: **click leadsto (single  $\vee$  double) within** [0, 1].

**Interpretation of patterns** we can use different formalisms to define the semantics of patterns. In this work, we focus on a denotational interpretation, based on first-order formulas over timed traces. We illustrate our approach using the pattern  $E_1$  **leadsto**  $E_2$  **within**  $I$ . For the “denotational” definition, we say that the pattern is true for a TTS  $N$  if and only if, for every timed-trace  $\sigma$  of  $N$ , we have:

$$\begin{aligned} \forall \sigma_1, \sigma_2 \ . \ (\sigma = \sigma_1 \pi_1 \sigma_2) & \Rightarrow \exists \sigma_3, \sigma_4 \ . \ \sigma_2 = \sigma_3 \pi_2 \sigma_4 \\ & \wedge \Delta(\sigma_3) \in I \wedge \pi_2 \notin \sigma_3 \end{aligned}$$

where  $\pi_1$  (resp.,  $\pi_2$ ) is an atomic proposition that matches all events containing a transition  $t$  whose label is  $E_1$  (resp.,  $E_2$ ). The denotational approach is very convenient for a “tool developer” (for instance to prove the soundness of an observer implementation in TTS) since it is self-contained and only relies on the definition of timed traces. As an alternative description of the pattern, we may use an MTL formula (see e.g. [20] for a definition of the logic):  $\Box(\pi_1 \Rightarrow (\neg \pi_2) \ \mathbf{U}_I \ \pi_2)$ , which reads like a LTL formula enriched by a time constraint on the **U** operator. An advantage of our pattern-based approach is that we do not

have to restrict to a particular decidable fragment of the logic. For example, we do not require that the interval  $I$  is not punctual (of the form  $[d, d]$ ); we add a pattern in our language only if we can provide a suitable observer for it, so that no decidability issue may arise. Last, we propose a graphical interpretation of patterns, mostly inspired by the Graphical Interval Logic (GIL) [11], called Time Graphical Interval Logic (TGIL), as pictured in the following diagram:



The diagram reads as a recipe (from top to bottom): from any point in time (marked with a  $\square$ ), if there exists an occurrence of the atomic proposition  $\pi_1$  in the future (take the first one), then there must exist a farther point for which  $\pi_2$  holds and the delay between these two points is in the interval  $I$ . Given this TGIL diagram and a TTS  $N$ , the property holds if and only if every timed-trace  $\sigma$  of  $N$  satisfies the recipe. This graphical representation is expected to be more convenient than MITL when explaining the semantics of patterns to non-expert.

## 4 Patterns Verification

We define different types of observers at the TTS level that can be used for the verification of patterns. (This classification is mainly informative, since nothing prohibits the mix of different types of observers.) We make use of the whole expressiveness of the TTS model: synchronous or asynchronous rendez-vous (through places and transitions); shared memory (through data variables); and priorities. The idea is not to provide a generic way of obtaining the observer from a formal definition of the pattern. Rather, we seek, for each pattern, to come up with the best possible observer in practice (see the discussion in Sect. 5).

### 4.1 Observers for the Leadsto Pattern

We focus on the example of the *leadsto* pattern. We assume that some transitions of the system are labeled with  $E_1$  and some others with  $E_2$ . We give three examples of observers for the pattern:  $E_1$  *leadsto*  $E_2$  within  $[0, max[$ , meaning that whenever  $E_1$  occurs, then (the first occurrence of)  $E_2$  must occur before  $max$  units of time. The first observer monitors transitions and uses a single place; the second observer monitors places; the third observer monitors shared, boolean variables injected into the system (by means of composition). While the use of places and transitions is traditionally favored when observing Petri Nets—certainly because of the definition of Petri Net composition—the use of a *data observer* is quite new in the context of TTS systems. The results of our experiments seem to show that, in practice, this is a promising way to implement an observer.

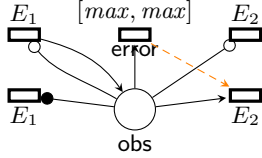


Fig. 4. Transition Observer

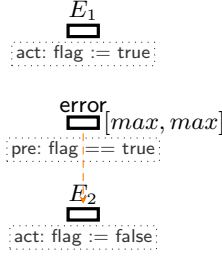


Fig. 5. Data Observer

**Transition Observer (Fig. 4)** the observer uses a place, *obs*, which records the time since the last transition labeled  $E_1$  occurred. We use a classical graphical notation for Petri Nets where arcs with a black circle denote *read arcs*, while arcs with a white circle are *inhibitor arcs*.

Place *obs* is emptied if a transition labeled  $E_2$  is fired otherwise the transition *error* is fired after  $max$  units of time. The (dashed) priority arc between *error* and  $E_2$  indicates that the transition  $E_2$  cannot fire if the transition *error* can fire; which mean that the property is not verified if the “first event”  $E_2$  after  $E_1$  occurs exactly after  $max$  units of time.

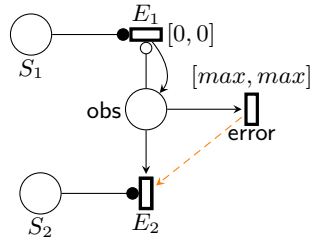
Proving that a TTS  $N$  satisfies this pattern amounts to checking that the system  $N \otimes O$  (where  $O$  is the observer) never reaches an event containing *error*. In the system displayed in Fig. 4, we use a *deterministic observer*, that examines all occurrences of  $E_1$  for the failure of a deadline.

By virtue of TTS composition (Def. 7), the observer in Fig. 4 duplicates each transition of  $N$  which is labeled  $E_1$  (respectively  $E_2$ ): one copy can be fired if *obs* is empty—as a result of the (white-circled) inhibitor arc—while the other can be fired only if the place is full. The transition *error* is fired if the place *obs* is full—there is an instance of  $E_1$ — and the interval  $[max, max]$  is elapsed. It is also possible to define a non-deterministic observer, such that some occurrences of  $E_1$  may be disregarded. This approach is safe since model-checking performs an exhaustive exploration of the TTS states, thus considering all possible scenarios. It is also quite close to the treatment obtained when compiling an (untimed) “equivalent LTL property”, namely  $\Box(E_1 \Rightarrow \Diamond E_2)$ , into an automaton [15]. Experiments have shown that the deterministic observer is more efficient, which underlines the benefit of singling out the best possible observer and looking for specific optimizations.

**Data observer (Fig. 5)** in this observer, the transition *error* is conditioned by the value of a variable “*flag*”. This shared boolean variable, which is initially set to false, is true between the firing of a transition  $E_1$  and the following transition  $E_2$ . Additionally, transition *error* is enabled only if *flag* is true. Therefore, like in the previous case, the verification of the pattern also boils down to checking the

reachability of the event `error`. Notice that the whole state of the data observer is encoded in its store, since the underlying net has no place.

**Place Observer (Fig. 6)** in this part, we assume that events  $E_1$  and  $E_2$  are associated to the system entering some given states  $S_1$  and  $S_2$ . We can easily adapt this net to observe events associated to transitions in the system. In our case, the observer will be composed with the system through its places  $S_1$  and  $S_2$  (we can extend the classic composition of Petri Nets over transitions to composition over places). In our observer, we use a transition labeled  $E_1$  whenever a token is placed in  $S_1$ . Note that TTS obtained from Fiacre are one-safe, meaning that at most one token may be in  $S_1$  at any given time. Likewise, we use a transition  $E_2$  for observing that the system is in state  $S_2$ . The error transition is fired if the observer stays in state `obs` for more than  $max$  units of time, as needed.



**Fig. 6.** Place Observer

## 4.2 Proving Innocuousness and Soundness of Observers

We start by giving sufficient conditions for an observer  $O$  to be *non-intrusive*, meaning that the observer does not interfere with the observed system. Formally, we show that any trace  $\sigma$  of the observed system  $N$  is preserved in the composed system  $N \otimes O$ : the observer does not obstruct a behavior of the system (see Lemma 1 below). Conversely, we show that, from any trace of the composition  $N \otimes O$ , we can obtain a trace of  $N$  by erasing the events from  $O$ : the observer does not add new behaviors to the system. This is actually a consequence of Property 1 (see Sect. 2.5).

We write  $T_{sync}$  the set of synchronized transitions of the observer (as defined in Def. 6). Let  $\rho$  be a state of the observer, and  $\sigma$  a trace such that there exists  $\rho'$  with  $\rho \xrightarrow{\sigma} \rho'$ . Then, we define  $O(\rho, \sigma)$  as the state  $\rho'$ , that is, the state reached after executing trace  $\sigma$  from state  $\rho$ . We use  $O(\sigma)$  as a shorthand for  $O(\rho_{init}, \sigma)$ , where  $\rho_{init}$  is the initial state. The following lemma states sufficient conditions for the observer to be non-intrusive.



**Lemma 1.** *Assume  $O$  satisfies the following conditions:*

- *For every  $t$  in  $T_{\text{sync}}$ ,  $\text{tc}(t) = [0; +\infty[$ , and  $t$  has no priority over other transitions.*
- *In every reachable state  $\rho$  of  $O$ , and for every  $l$  in  $\text{lab}(T_{\text{sync}})$ , there exists a (possibly empty) finite trace  $\sigma$  not containing transitions in  $T_{\text{sync}}$  such that  $\Delta(\sigma) = 0$  and there exists  $t \in T_{\text{sync}}$  with  $\text{lab}(t) = l$ , which is fireable in state  $O(\rho, \sigma)$ .*
- *There exists  $\delta > 0$  such that, in every reachable state  $\rho$  of  $O$ , there exists a (possibly empty) finite trace  $\sigma$  not containing transitions in  $T_{\text{sync}}$  with  $\rho \xrightarrow{\sigma^{d(\delta)}}$ .*

*Then, for all  $\sigma_1$  in  $\Sigma(N)$  there exists  $\sigma_2$  in  $\Sigma(O)$  such that  $\sigma_1$  and  $\sigma_2$  are composable.*

A few comments: first condition is necessary for composition (as required by Def. 6). Second condition ensures that the observer does not prevent the firing of a ( $l$ -labeled) synchronized transition for more than 0 units of time. Note also that the observer cannot involve other synchronized transitions while reaching a state where  $l$  is fireable, since this would abusively constrain the behavior of the main system—not to mention deadlock issues. Third condition ensures that the observer may always let time significantly elapse, without requiring synchronized transitions either (for the same reason).

From the compositionality property (Property 1, Sect. 2.5), it follows that the composed trace  $\sigma_1 \otimes \sigma_2$  belongs to  $\Sigma(N \otimes O)$ , which means that every valid behavior  $\sigma_1$  of the observed system  $N$  is also present in the behavior of  $N \otimes O$ .

*Proof.* We assume  $O$  satisfies the given hypotheses. We have to build a trace  $\sigma_2$  in  $\Sigma(O)$  such that  $\sigma_1 \bowtie \sigma_2$ . Since traces are considered up to equivalence, we actually build two traces  $\sigma_2$  and  $\sigma_3$  such that both  $\sigma_2 \bowtie \sigma_3$  and  $\sigma_1 \equiv \sigma_3$  hold:

*For all  $\sigma_1$  in  $\Sigma(N)$ , there exist  $\sigma_2$  in  $\Sigma(O)$  and  $\sigma_3$  in  $\Sigma(N)$  such that  $\sigma_1 \equiv \sigma_3$ , and for all  $t > 0$ , for all  $\sigma_3^a$  finite prefix of  $\sigma_3$  with  $\Delta(\sigma_3^a) < t$ , there exists  $\sigma_2^a$  finite prefix of  $\sigma_2$  such that  $\sigma_2^a \bowtie \sigma_3^a$  holds.*

We provide an algorithm  $f$  that builds  $\sigma_2$  and  $\sigma_3$  incrementally.

- The inputs of  $f$  are  $\sigma_1$ ,  $\sigma_1^a$ ,  $\sigma_2^a$  and  $\sigma_3^a$ . They must satisfy the following:  $\sigma_1 \equiv \sigma_3^a \sigma_1^a$  holds, as well as  $\sigma_2^a \bowtie \sigma_3^a$ . Intuitively,  $\sigma_3^a$  is the part of  $\sigma_1$  (up to equivalence) that has already been done, whereas  $\sigma_1^a$  is the part remaining to be considered.
- The algorithm returns a new triple  $\sigma_1^b$ ,  $\sigma_2^b$  and  $\sigma_3^b$ , which satisfies similar conditions, and such that  $\sigma_2^a$  and  $\sigma_3^a$  are prefixes of  $\sigma_2^b$ , and  $\sigma_3^b$  respectively.
- The algorithm is invoked iteratively with the returned triple. In the finite case (when  $\sigma_1$  is finite), it eventually reaches a point where  $\sigma_1^a$  is empty, in which case  $\sigma_1 \equiv \sigma_3^a$  holds. In the infinite case, we take  $\sigma_2$  as the limit of  $\sigma_2^b$ , and  $\sigma_3$  as the limit of  $\sigma_3^b$ .

We now provide the details of the algorithm, then we consider its soundness, being careful with respect to well-formedness conditions (checking in particular that the algorithm does not pile up infinite sequences of zero-delay events).

*Algorithm*  $f(\sigma_1, \sigma_1^a, \sigma_2^a, \sigma_3^a)$  : let  $x$  and  $\sigma'_1$  be such that  $\sigma_1^a$  equals  $x\sigma'_1$ . With no loss of generality, we may freely assume that  $x$  is not  $d(0)$ . We proceed by case on  $x$ :

- (a) If  $x$  is an event  $(t, m, s)$  with  $t \notin T_{sync}$ , then we return  $\sigma_1^b = \sigma'_1$ ,  $\sigma_2^b = \sigma_2^a d(0)$ , and  $\sigma_3^b = \sigma_3^a x$ .
- (b) If  $x$  is an event  $(t, m, s)$  with  $t \in T_{sync}$ , then by hypothesis on  $O$ , there exists a finite trace  $\sigma$  not containing transitions in  $T_{sync}$  such that  $\Delta(\sigma) = 0$ ,  $\sigma_2^a \sigma \in \Sigma(O)$  and  $t'$  is fireable in  $O(\sigma_2^a \sigma)$  with  $\text{lab}(t') = \text{lab}(t)$ . Let  $\sigma'$  be the sequence with the same length as  $\sigma$  and whose elements are  $d(0)$ . Let  $\omega$  be  $(t', m', s')$  where  $m'$  and  $s'$  are an appropriate marking and state such that  $\sigma_2^a \sigma \omega$  is in  $\Sigma(O)$ . Then, we return  $\sigma_1^b = \sigma'_1$ ,  $\sigma_2^b = \sigma_2^a \sigma \omega$ , and  $\sigma_3^b = \sigma_3^a \sigma' x$ .
- (c) If  $x$  is  $d(\delta)$ , then by hypothesis on  $O$ , there exists  $\delta_2 > 0$  and a finite trace  $\sigma$  not containing transitions in  $T_{sync}$  such that  $\sigma_2^a \sigma d(\delta_2)$  is in  $\Sigma(O)$ . Let  $\sigma'$  be the sequence with the same length as  $\sigma$  and whose elements are  $d(0)$  or  $d(\delta'_i)$ , with appropriate  $\delta'_i$  such that  $\sigma' \bowtie \sigma$  holds. We distinguish two subcases:
  - (i) either  $\delta \leq \Delta(\sigma) + \delta_2$ , in which case we return  $\sigma_1^b = \sigma'_1$ ,  $\sigma_2^b = \sigma_2^a \sigma d(\delta - \Delta(\sigma))$  and  $\sigma_3^b = \sigma_3^a \sigma' d(\delta - \Delta(\sigma))$  provided  $\delta - \Delta(\sigma) \geq 0$ . If  $\delta - \Delta(\sigma) < 0$ , we have to truncate both  $\sigma$  and  $\sigma'$  at duration  $\delta$  (omitting the details).
  - (ii) either  $\Delta(\sigma) + \delta_2 < \delta$ , in which case we return  $\sigma_1^b = d(\delta - \delta_2)\sigma'_1$ ,  $\sigma_2^b = \sigma_2^a \sigma d(\delta_2)$ , and  $\sigma_3^b = \sigma_3^a \sigma' d(\delta_2)$ .

There is no difficulty in checking that, for each case, the returned triple satisfies the output conditions, that is,  $\sigma_1 \equiv \sigma_3^b \sigma_1^b$  and  $\sigma_2^b \bowtie \sigma_3^b$ , as long as  $\sigma_1^a$ ,  $\sigma_1^b$ , and  $\sigma_1^c$  satisfy the input conditions, that is,  $\sigma_1 \equiv \sigma_3^a \sigma_1^a$  and  $\sigma_2^a \bowtie \sigma_3^a$ .

This implies that  $\sigma_2 \bowtie \sigma_3$  holds (both in the finite and infinite case). However, care must be taken to show that  $\sigma_1 \equiv \sigma_3$  holds in the infinite case (the finite case being immediate). To prove this last point, we now consider  $\sigma_1$  infinite, which implies  $\Delta(\sigma_1) = \infty$  by well-formedness of  $\sigma_1$ . Thus, we only have to show that  $\Delta(\sigma_3) = \infty$  (that is,  $\sigma_3$  is well-formed), which implies  $\sigma_1 \equiv \sigma_3$  (omitting the details). This is proven by means of contradiction: assume  $\Delta(\sigma_3)$  is finite, although  $\sigma_3$  is infinite. Then, necessarily, at least one case (or subcase) of the algorithm is repeated an infinite number of steps. It cannot be subcase (ii) because  $\delta_2$  is a positive constant, and thus  $d(\delta_2)$  cannot occur an infinite number of times in  $\sigma_3$ , whose duration is finite. As a consequence, after a finite number of iterations, all delays  $d(\delta)$  occurring in  $\sigma_1$  are handled by subcase (i). It cannot be subcase (i) either, because otherwise  $\Delta(\sigma_1)$  would also be finite. It cannot be cases (a) nor (b) either, because otherwise  $\sigma_1$  would end with an infinite sequence of events  $(t, m, s)$ , with no delay, which would imply  $\Delta(\sigma_1)$  is finite.

The conditions in Lemma 1 are true for the implementation of the leadsto observer, defined in Fig. 4 and in Fig. 5. Therefore these observers cannot interfere with the system under observation. Next, we prove that the transition observer is sound, meaning that it reports correctly if its associated pattern is valid or not. We prove the soundness of this observer by showing that, for any TTS  $N$ , the event `error` does not appear in the traces of  $N \otimes O$  if and only if

the pattern is valid for  $N$ . We write  $\mathbf{error} \in N \otimes O$  to mean there exists a trace  $\sigma \otimes \sigma'$  in  $\Sigma(N \otimes O)$  such that  $\mathbf{error} \in \sigma'$ .

**Lemma 2.** *We have  $\mathbf{error} \notin N \otimes O$  if and only if for all  $\sigma \in \Sigma(N)$  such that  $\sigma = \sigma_1 \omega_1 \sigma_2$  for some traces  $\sigma_1, \sigma_2$  and  $\omega_1$  with  $\mathbf{lab}(\omega_1) = E_1$ , there exist  $\sigma_3, \omega_2$ , and  $\sigma_4$  with  $\sigma_2 = \sigma_3 \omega_2 \sigma_4$ ,  $\mathbf{lab}(\omega_2) = E_2$ , and  $\Delta(\sigma_3) < \max$ .*

*Proof.* This is a consequence of the following result, where for any trace  $\sigma$ , we write  $\mathbf{lab}(\sigma)$  for the set of labels occurring in  $\sigma$ , that is  $\cup_{i \in \text{dom } \sigma} \mathbf{lab}(\sigma(i))$ .

**Result 1** *Assume  $\sigma_1 \in \Sigma(N)$  and  $\sigma_2 \in \Sigma(O)$  with  $\sigma_1 \bowtie \sigma_2$ . We additionally assume that  $\sigma_1$  and  $\sigma_2$  are maximal, that is, there is no traces  $\sigma_1 \sigma'_1 \in \Sigma(N)$  and  $\sigma_2 \sigma'_2 \in \Sigma(O)$  such that  $\sigma_1 \sigma'_1 \bowtie \sigma_2 \sigma'_2$  holds. Under these hypotheses, we have  $\mathbf{error} \in \sigma_2$  if and only if there exist  $\sigma_1^a, \omega_1, \sigma_1^b$ , and  $\sigma_1^c$  such that  $\sigma_1 = \sigma_1^a \omega_1 \sigma_1^b \sigma_1^c \wedge \mathbf{lab}(\omega_1) = E_1 \wedge \Delta(\sigma_1^b) \geq \max \wedge E_2 \notin \mathbf{lab}(\sigma_1^b)$ .*

*Proof.* We first show the “if” way. We define three subcases: either  $\Delta(\sigma_1^c) = 0$  (subcase i), or, without loss of generality, we may freely assume that either  $\Delta(\sigma_1^b) > \max$  (subcase ii), or that the first event of  $\sigma_1^c$  is labeled with  $E_2$  (subcase iii). In all these subcases, since  $\sigma_1 \bowtie \sigma_2$  holds,  $\sigma_2$  is necessarily of the form  $\sigma_2^a \omega_2 \sigma_2^b \sigma_2^c$  with  $\sigma_1^a \bowtie \sigma_2^a, \omega_1 \bowtie \omega_2, \sigma_1^b \bowtie \sigma_2^b$ , and  $\sigma_1^c \bowtie \sigma_2^c$  (as a consequence of Definition 8). This implies  $\mathbf{lab}(\omega_2) = E_1, \Delta(\sigma_2^b) = \Delta(\sigma_1^b) \geq \max$  and  $E_2 \notin \mathbf{lab}(\sigma_2^b)$ . Additionally, either  $\Delta(\sigma_2^c) = 0$  (subcase i holds), or  $\Delta(\sigma_2^b) > \max$  (subcase ii), or the first event of  $\sigma_2^c$  is labeled with  $E_2$  (subcase iii). Let  $\rho$  be  $O(\sigma_2^a \omega_2)$ . By construction of the observer,  $\mathbf{error}$  is necessarily enabled in state  $\rho$ . Also by construction, only the firing of  $\mathbf{error}$  or the firing of  $E_2$  may disable  $\mathbf{error}$ . Moreover, the time constraint on  $\mathbf{error}$  ensures that it cannot remain enabled continuously for more than  $\max$  units of time. We now consider the three subcases defined above:

- Subcase(i) : we have  $\Delta(\sigma_2^c) = 0$ . Necessarily,  $\mathbf{error}$  must be fired in  $\sigma_2^b$ , otherwise  $\mathbf{error}$  would be fireable at the end of  $\sigma_2$ , which is in contradiction with the hypothesis that  $\sigma_1$  and  $\sigma_2$  are maximal.
- Subcase(ii) : we have  $\Delta(\sigma_2^b) > \max$ . Since  $E_2$  is not fired in  $\sigma_2^b$ , then  $\mathbf{error}$  must be fired in  $\sigma_2^b$ , that is,  $\mathbf{error} \in \sigma_2$ .
- Subcase(iii) : we have  $\Delta(\sigma_2^b) = \max$ , and the first event of  $\sigma_2^c$  is  $E_2$ . As a consequence,  $\mathbf{error}$  cannot be fireable in  $O(\sigma_2^a \omega_2 \sigma_2^b)$  because it would have priority over the next event to come, namely  $E_2$ , which is a contradiction with the semantics. Thus,  $\mathbf{error}$  must be fired in  $\sigma_2^b$ , that is,  $\mathbf{error} \in \sigma_2$ .

In all cases, we see that  $\mathbf{error}$  is fired in  $\sigma_2^b$ . This concludes the “if” way.

Conversely (“only if” way), we assume that  $\mathbf{error} \in \sigma_2$ . By construction of the observer,  $\mathbf{error}$  must have been enabled for  $\max$  units of time, that is  $\sigma_2 = \sigma_2^a \sigma_2^b \omega_3 \sigma_2^c$ , with  $\mathbf{lab}(\omega_3) = \mathbf{error}, \Delta(\sigma_2^b) = \max$ , and  $\mathbf{error}$  is enabled in all events of  $\sigma_2^b$ . Without loss of generality, we may take  $\sigma_2^b$  as large as possible, which implies that it starts with the first event that enabled  $\mathbf{error}$ .  $\sigma_2^b = \omega_2 \sigma_2^b$ , where  $\mathbf{lab}(\omega_2) = E_1$ , necessarily. Additionally, since  $\mathbf{error}$  is kept enabled for all events of  $\sigma_2^b$ , we must have  $E_2 \notin \mathbf{lab}(\sigma_2^b)$ . Finally, since  $\sigma_1 \bowtie \sigma_2$  holds, there exist  $\sigma_1^a$ ,

$\omega_1, \sigma_1^b, \sigma_1^c$  with  $\sigma_1 = \sigma_1^a \omega_1 \sigma_1^b \sigma_1^c$ ,  $\sigma_1^a \bowtie \sigma_2^a$ ,  $\omega_1 \bowtie \omega_2$ ,  $\sigma_1^b \bowtie \sigma_2^b$  and  $\sigma_1^c \bowtie \sigma_2^c$ . As a consequence,  $\text{lab}(\omega_1) = E_1$ ,  $\Delta(\sigma_1^b) = \text{max}$ , and  $E_2 \notin \text{lab}(\sigma_1^b)$ . This concludes the proof.

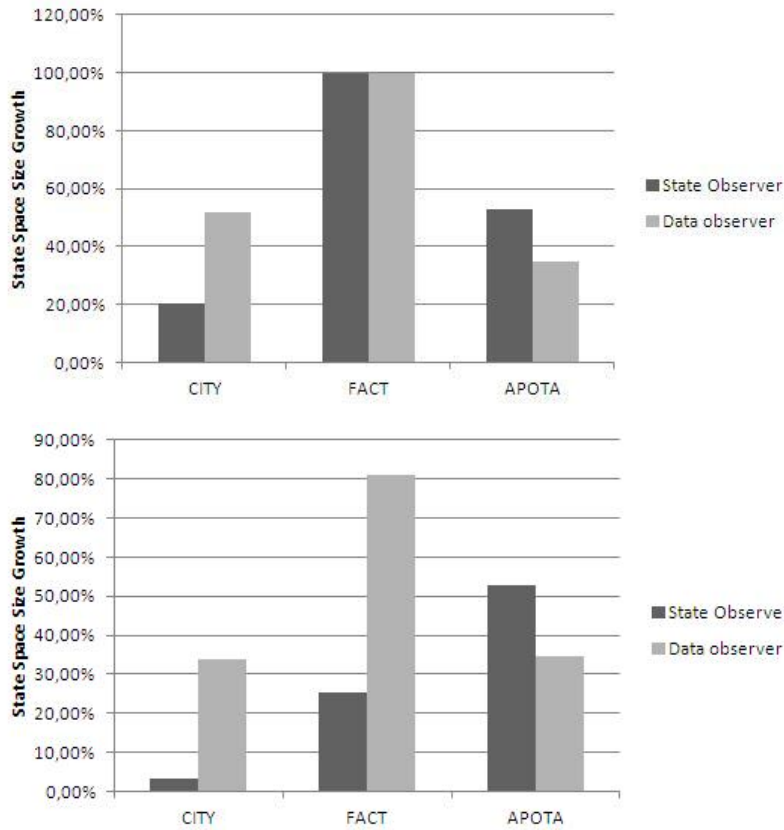
## 5 Experimental Results

Our verification framework has been integrated into a prototype extension of *frac*, the Fiacre compiler for the TINA toolbox. This extension supports the addition of real-time patterns and automatically compose a system with the necessary observers. (The software is available at <http://homepages.laas.fr/~nabid>.) In case the system does not meet its specification, we obtain a counterexample that can be converted into a timed sequence of events exhibiting a problematic scenario. This sequence can be played back using *nd*, the Time Petri Net animator provided by TINA.

We define the *empirical complexity* of an observer as its impact on the augmentation of the state space size of the observed system. For a system  $S$ , we define  $\text{size}(S)$  as the size (in bytes) of the *State Class Graph* (SCG) [9] of  $S$  generated by our verification tools. In our verification tools, we use SCG as an abstraction of the state space of a TTS. State class graphs exhibit good properties: an SCG preserves the set of discrete traces—and therefore preserves the validation of LTL properties—and the SCG of  $S$  is finite if the Petri Net associated to  $S$  is bounded and if the set of values generated from  $S$  is finite. We cannot use the “plain” labeled transition system associated to  $S$  to define the size of  $S$ ; indeed, this transition graph maybe infinite since we work with a dense time model and we have to take into account the passing of time.

The size of  $S$  is a good indicator of the memory footprint and the computation time needed for model-checking the system  $S$ : the time and space complexity of the model-checking problem is proportional to  $\text{size}(S)$ . Building on this definition, we say that the complexity of an observer  $O$  applied to the system  $S$ , denoted  $C_O(S)$ , is the quotient between the size of  $(S \otimes O)$  and the size of  $S$ .

We resort to an empirical measure for the complexity since we cannot give an analytical definition of  $C_O$  outside of the simplest cases. However, we can give some simple bounds on the function  $C_O$ . First of all, since our observers should be non-intrusive (see Sect. 4.2), we can show that the SCG of  $S$  is a subgraph of the SCG of  $S \otimes O$ , and therefore  $C_O(S) \geq 1$ . Also, in the case of the *leadsto* pattern, the transitions and places-based observers add exactly one place to the net associated to  $S$ . In this case, we can show that the complexity of these two observers is always less than 2; we can at most double the size of the system. We can prove a similar upper bound for the *leadsto* observer based on data. While the three observers have the same (theoretical) worst-case complexity, our experiments have shown that one approach was superior to the others. We are not aware of previous work on using experimental criteria to select the best observer for a real-time property. In the context of “untimed properties”, this approach may be compared to the problem of optimizing the generation of Büchi Automata from LTL formulas, see e.g. [15].



**Fig. 7.** Complexity for the data and state observer classes in percentage of system size growth—average time for invalid properties (above) and valid properties (below).

We have used our prototype compiler to experiment with different implementations for the observers. The goal is to find the most efficient observer “in practice”, that is the observer with the lowest complexity. To this end, we have compared the complexity of different implementations on a fixed set of representative examples and for a specific set of properties (we consider both valid and invalid properties). The results for the `leadsto` pattern are displayed in Fig. 7. For the experiments used in this paper, we use three examples of TTS selected because they exhibit very different features (size of the state space, amount of concurrency and symmetry in the system, ...). Example CITY is a TTS obtained from a business workflow describing the delivery of identity documents in a French city hall. In this example, timing constraints arise from delays in the communication between services and time spent to perform administrative procedures. The valid property, in this case, states that the minimal possible delay for obtaining an id is 30 hours. This is a typical `leadsto` pattern that can

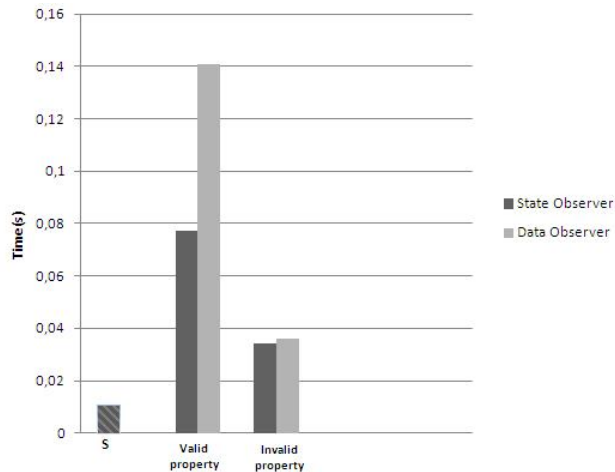
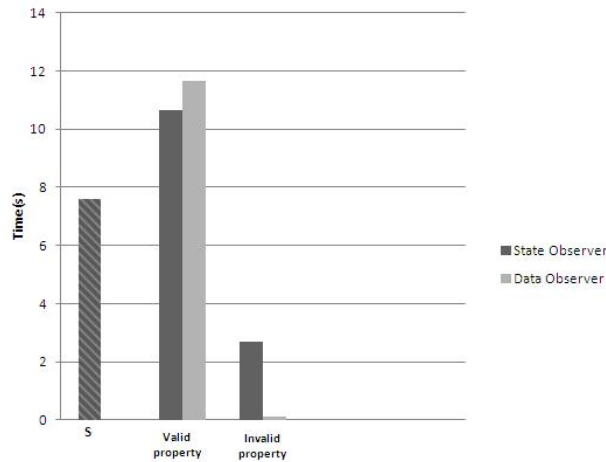


Fig. 8. Total verification time (factory example)

be written: **dfleadsto pf inlessthan** 30, where **df** is a state corresponding to the start of the process and **pf** is a state corresponding to the delivery of the document to the applicant. The same property, with a minimum delay set to 100 instead of 30, gives our example of invalid property. Example FACT is a TTS modeling a manufacturing plant composed of two command lines sharing some of theirs machines. In this case, timing constraints arise from a combination of safety issues—workers should not work more than 35 minutes in a row—and performance issues—machines perform a task in a time between 5 and 10 minutes and should be maintained after 15 cycles. The valid property, for the FACT example, states that the delay between two successive breaks should not exceed 35 minutes. For the invalid property, we use the same requirement, but shortening the delay to 5 minutes. The last example, APOTA, is an industrial use case that models the dynamic architecture for a network protocol in charge of data communications between an airplane and ground stations [6]. In this case, timing constraints arise from timeouts between requests and periods of the tasks involved in the protocol implementation. The property, in this case, is related to the worst-case execution time for the main application task.

In Fig. 7, we compare the growth in the state space size—that is the value of  $C_o(S)$ —for the place and data observers defined in Sect. 4.1 and our three running examples. We give one figure in the case where the property is not valid and another when the property is valid. We have compared also, in Fig. 8 and 9, the total verification time for the FACT and APOTA examples. This time refers to the time spend generating the complete state space of the system and verifying the property. In Fig. 8 and 9,  $S$  refers to the initial system (the state space of the system without adding observer) while “Valid property” and



**Fig. 9.** Total verification time (APOTA example)

“Invalid property” refer to the state space of the system synchronized with data observer and state observer in the case of valid and unvalid property respectively.

In our experiments, we have consistently observed that the observer based on data is the best choice; it is the observer giving the minimal execution time in average and that seldom gives the worst result. Although the diagrams shown above do not seem in favor of data observers, we have carried out other numerous tests which actually show promising results for data observers. As a matter of fact, the few poor results of the data observer can be explained by pathological cases where the time parameters used in the property are very different from those used in the system (a classical problem whith model-checking real-time systems.)

## 6 Related Work, Contributions and Perspectives

Two broad approaches coexist for the definition and verification of real-time properties: (1) real-time extensions of temporal logic [17]; and (2) observer-based approaches, such as the Context Description Languages (CDL) of Dhaussy et al. [22] or approaches based on timed automata [20,3,2].

Obviously, the logic-based approach provides most of the theoretically well-founded body of works, such as complexity results for different fragments of real-time temporal logics [17]: Temporal logic with clock constraints (TPTL); Metric Temporal Logic—with or without interval constrained operators—; Event Clock Logic; etc. The algebraic nature of logic-based approaches make them expressive and enable an accurate formal semantics. However, it may be impossible to express all the necessary requirements inside the same logic fragment if we ask

for an efficient model-checking algorithm (with polynomial time complexity). For example, Uppaal [4] chose a restricted fragment of TCTL with clock variables, while Kronos provide a more expressive framework, but at the cost of a much higher complexity. As a consequence, selecting this approach requires to develop model-checkers for each interesting fragment of these logics—and a way to choose the right tool for every requirement—which may be impractical.

Pattern-based approaches propose a user-friendly syntax that facilitates their adoption by non-experts. However, in the real-time case, most of these approaches lack in theory or use inappropriate definitions. One of our goal is to reverse this situation. In the seminal work of Dwyer et al. [12], patterns are defined by translation to formal frameworks, such as LTL and CTL. There is no need to provide a verification approach, in this case, since efficient model-checkers are available for these logics. This work on patterns has been extended to the real-time case. For example, Konrad et al. [19] extends the patterns language with time constraints and give a mapping from timed pattern to TCTL and MTL, but they do not study the decidability of the verification method (the implementability of their approach). Another related work is [16], where the authors define observers based on Timed Automata for each pattern. However, they do not provide a formal framework for proving the correctness or the innocuousness of their observers and they have not integrated their approach inside a model-checking toolchain.

Concerning observer-based approaches, we can cite the work of Aceto et al. [2,3] where test automata are used to check properties of reactive systems. The goal is to identify properties on timed automata for which model checking can be reduced to reachability checking. In this framework, verification is limited to safety and bounded liveness properties. In the context of Time Petri Net, a similar approach has been experimented by Toussaint et al. [23], but they propose a less general model for observers and consider only two verification techniques over four kinds of time constraints.

In contrast to these related works, we make the following contributions. We reduce the problem of checking real-time properties to the problem of checking LTL properties on the composition of the system with an observer. This paper provides several theoretical results: we give the first formal account of the semantics of TTS—a low-level model used in the TINA toolset—and provide a formal framework for proving the correctness of observers. We use also this framework to check whether an observer is non-intrusive—whether it can interfere with the behaviour of the system under observation—a property that we call *innocuousness*. To the best of our knowledge, this property is totally overlooked in the related work on observer-based approaches. Moreover, we give necessary conditions for an observer to be innocuous (see Lemma 1 in Sect. 4.2).

Our approach has been integrated into a complete verification toolchain for the Fiacre modeling language and can therefore be used in conjunction with Topcased. We give several experimental results based on the use of this toolchain in Sect. 4. The fact that we implemented our approach has influenced our definition of the observers. Indeed, another contribution of our work is the use of



a pragmatic approach for comparing the effectiveness of different observers for the same property. Our experimental results seem to show that data observers look promising.

We are following several directions for future work. A first goal is to define a new low-level language for observers—adapted from the TTS model—equipped with more powerful optimization techniques and with easier soundness proofs. On the theoretical side, we are currently looking into the use of mechanized theorem proving techniques to support the validation of observers. On the experimental side, we need to define an improved method to select the best observer. For instance, we would like to provide a tool for the “syntax-directed selection” of observers that would choose (and even adapt) the right observers based on a structural analysis of the target system.

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## A Real-time Patterns Language

We present bellow our real-time patterns language as well as a textual definition for each patterns. More details about these patterns are provided in [1].

Table 1: Existence patterns

<p>1. Present <math>A</math> after <math>B</math> within <math>[d_1, d_2]</math></p> <div style="border: 1px solid black; padding: 10px; margin: 10px 0;"> <p>– <b>Textual Definition:</b> An event, say <math>A</math>, must occur between <math>d_1</math> and <math>d_2</math> units of time (u.t) after an occurrence of the event <math>B</math>. The pattern is also satisfied if <math>B</math> never occurs.</p> </div>
<p>2. Present first <math>A</math> before <math>B</math> within <math>[d_1, d_2]</math></p> <div style="border: 1px solid black; padding: 10px; margin: 10px 0;"> <p>– <b>Textual Definition:</b> The first occurrence of <math>A</math> holds within <math>[d_1, d_2]</math> u.t. before the first occurrence of <math>B</math>. It also holds if <math>B</math> does not occur.</p> </div>
<p>3. Present <math>A</math> lasting <math>D</math></p> <div style="border: 1px solid black; padding: 10px; margin: 10px 0;"> <p>– <b>Textual Definition:</b> The goal of this pattern is to assert that from the first occurrence of <math>A</math>, the predicate <math>A</math> remains true for at least duration <math>D</math>. It makes sense only if <math>A</math> is a state predicate (that is, on the marking and store), and which does not refer to any transition (since transitions are instantaneous, we cannot require a transition to last for a given duration).</p> </div>
<p>4. Present <math>A</math> within <math>I</math></p> <div style="border: 1px solid black; padding: 5px; margin: 10px 0;"> <p>This pattern is equivalent to <b>present A after init within I</b></p> </div>
<p>5. Present <math>A</math> between <math>B</math> and <math>C</math> within <math>I</math></p> <div style="border: 1px solid black; padding: 10px; margin: 10px 0;"> <p>This pattern is equivalent to the composition of two patterns :  <b>present A after B within I</b>  <b>and</b>  <b>present A before C within I</b></p> </div>
<p>6. Present <math>A</math> after <math>B</math> until <math>C</math> within <math>I</math></p> <div style="border: 1px solid black; padding: 5px; margin: 10px 0;"> <p>This pattern is equivalent to: <b>A leadsto C within I after B</b></p> </div>

Table 2: Absence patterns

1. Absent $A$ after $B$ for interval $[d_1, d_2]$
<p>– <b>Textual Definition:</b> This pattern asserts that an event, say <math>A</math>, must not occur between <math>d_1</math>–<math>d_2</math> u.t. after the first occurrence of an event <math>B</math>. This pattern is dual to <b>Present <math>A</math> After <math>B</math> within <math>[d_1, d_2]</math></b> (but it is not strictly equivalent to its negation, because in both patterns, <math>B</math> is not required to occur).</p>
2. Absent $A$ before $B$ for duration $D$
<p>– <b>Textual Definition:</b> This pattern asserts that no <math>A</math> can occur less than <math>D</math> u.t. before the first occurrence of <math>B</math>.</p>
3. Absent $A$ within $I$
<p>This pattern is defined as <b>Absent <math>A</math> after init within <math>I</math></b></p>
4. Absent $A$ lasting $D$
<p>This pattern is defined as <b>Present <math>\neg A</math> lasting <math>D</math></b></p>
5. Absent $A$ between $B$ and $C$ within $I$
<p>This pattern is equivalent to the composition of two patterns :  <b>absent <math>A</math> after <math>B</math> within <math>I</math></b>  <b>and</b>  <b>absent <math>A</math> before <math>C</math> within <math>I</math></b></p>
6. Absent $A$ after $B$ until $C$ within $I$
<p>This pattern is equivalent to : <b>absent <math>A \wedge C</math> after <math>B</math> within <math>I</math></b></p>

Table 3: Response patterns

<b>Response Patterns</b>
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1. $A$ leadsto first $B$ within $[d_1, d_2]$
<p>– <b>Textual Definition:</b> This pattern states that every occurrence of an event, say <math>A</math>, must be followed by an occurrence of <math>B</math> within a time interval <math>[d_1, d_2]</math> (considering only the first occurrence of <math>B</math> after <math>A</math>).</p>
2. $A$ leadsto first $B$ within $[d_1, d_2]$ before $R$
<p>– <b>Textual Definition:</b> This pattern asserts that, before the first occurrence of <math>R</math>, each occurrence of <math>A</math> is followed by <math>B</math>, which occurs both before <math>R</math>, and in the time interval <math>[d_1, d_2]</math> after <math>A</math>. If <math>R</math> does not occur, the pattern holds.</p>
3. $A$ leadsto first $B$ within $[d_1, d_2]$ after $R$
<p>– <b>Textual Definition:</b> This pattern asserts that after the first occurrence of <math>R</math>, “<math>A</math> leadsto first <math>B</math> within <math>[d_1, d_2]</math>” holds.</p>
4. $A$ leadsto $B$ between $Q$ and $R$ within $I$
<p>This pattern is equivalent to the composition of two patterns :  <b>A leadsto B within I after Q</b>  <b>and</b>  <b>A leadsto B within I before R</b></p>
5. $A$ leadsto $B$ after $Q$ until $R$ within $I$
<p>This pattern is equivalent to : <b>A leadsto B between Q and R within I</b></p>

Table 4: Universality patterns

1. always $A$ lasting $D$
<p>This pattern is defined as <b>Present A lasting D</b></p>

2. always $A$ within $I$
This pattern is defined as $\neg(\mathbf{absent} \ A \ \mathbf{after} \ \mathbf{init} \ \mathbf{for} \ \mathbf{interval} \ I)$
3. always $A$ after $B$ for duration $D$
This pattern is defined as $\mathbf{absent} \ \neg A \ \mathbf{after} \ B \ \mathbf{for} \ \mathbf{duration} \ D$
4. always $A$ before $B$ for duration $D$
This pattern is defined as $\mathbf{absent} \ \neg A \ \mathbf{before} \ B \ \mathbf{for} \ \mathbf{duration} \ D$

Table 5: Precedence patterns

1. $A$ precedes $B$ for duration $D$
This pattern is defined as $\mathbf{absent} \ B \ \mathbf{before} \ A \ \mathbf{for} \ \mathbf{duration} \ D$
2. $A$ precedes $B$ before $R$ for duration $D$
<p>– <b>Textual Definition:</b> This pattern asserts that before the first occurrence of <math>R</math>, no <math>B</math> occurs before the first occurrence of <math>A</math> for duration <math>D</math>.</p>
3. $A$ precedes $B$ after $R$ for duration $D$
<p>– <b>Textual Definition:</b> This pattern asserts that before the first occurrence of <math>R</math>, no <math>B</math> occurs before the first occurrence of <math>A</math> for duration <math>D</math>.</p>
4. $A$ precedes $B$ between $Q$ and $R$ for duration $D$
This pattern is equivalent to the composition of two patterns : $A$ <b>precedes</b> $B$ <b>after</b> $Q$ <b>for duration</b> $D$ <b>and</b> $A$ <b>precedes</b> $B$ <b>before</b> $R$ <b>for duration</b> $D$
5. $A$ precedes $B$ after $Q$ until $R$ for duration $D$

This pattern is equivalent to : **absent B between Q and R for duration D**